



AIDA-PEx: Parasitic Extraction on Layout-Aware Analog Integrated Circuit Sizing

Bruno Cambóias Cardoso

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Supervisors

Prof. Nuno Cavaco Gomes Horta

Eng. Pedro Miguel Leite Cordeiro Ventura

Eng. Ricardo Miguel Ferreira Martins

Examination Committee

Chairperson: Prof. Horácio Cláudio Campos Neto

Supervisor: Prof. Nuno Cavaco Gomes Horta

Member of the Committee: Prof. Rui Santos-Tavares

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Abstract

The work presented in this dissertation belongs to the scientific area of electronic design automation (EDA) and addresses the parasitic extraction in automatic sizing of analog integrated circuits (ICs). The proposed innovative parasitic extractor, henceforward called AIDA-PEx, was developed to be embedded in an in-house automatic layout-aware analog IC synthesis tool, AIDA, and has the main goal of providing accurate parasitic estimates to lead and accelerate the layout/parasitic-aware optimization of the circuit. Finding a circuit sizing solution that fulfills all performance specifications after circuit layout is a time-consuming task that requires non-systematic iterations between electrical and physical design steps, which increases the design time of analog ICs. Moreover, the performance of automatic layout-aware IC sizing methodologies is heavily dependent on the promptitude of the iterations. The in-loop evaluation of each tentative solution encompasses three main steps: circuit simulation, layout generation and parasitic extraction. The proposed approach, unlike previous approaches available in the literature, estimates the parasitic capacitances and resistances from a simplified layout that includes the floorplan and a non-detailed routing, using an empirical-based method supported by the data from the technology design kit (TDK) files. AIDA-PEx uses the provided empirical data and geometrical considerations to model the parasitic components of the devices' terminals and routing paths for a complete 2.5-D extraction. Experimental results are presented for the United Microelectronics Corporations (UMC) 0.13 μ m design process and compared with the industry standard parasitic extractor Mentor Graphics' Calibre®, which showed that 90% of the solutions needed the layout-aware approach to assure a correct post-layout simulation that meets all the specifications.

Keywords

Analog Integrated Circuits Design

Computer-Aided Design

Electronic Design Automation

Layout-Aware Circuit Sizing

Parasitic Extraction

Resumo

O trabalho descrito nesta dissertação enquadra-se na área científica de automação de projecto eletrónico, e foca a extração de parasitas no contexto do dimensionamento automático dos componentes de circuitos integrados analógicos. Encontrar uma solução para o dimensionamento do circuito que cumpra todas as especificações de performance depois da geração do *layout* é um processo demorado, que necessita de iterações não sistemáticas entre fases de projeto elétricas e físicas, o que aumenta bastante o tempo de desenvolvimento do projeto. No entanto, a performance de metodologias automáticas de dimensionamento de circuitos integrados com inclusão de componentes do layout é extremamente dependente da rapidez de execução das iterações. A avaliação de cada solução encontrada dentro do ciclo de otimização engloba três etapas principais: simulação do circuito, geração do *layout* e extração de parasitas. O extrator de parasitas proposto, denominado AIDA-PEx, foi desenvolvido com o intuito de ser embebido numa ferramenta de dimensionamento automático de circuitos integrados analógicos que inclui informação do *layout* durante a otimização, AIDA. O AIDA-PEx tem como objetivo principal fornecer estimativas precisas de componentes parasitas de modo a conduzir rapidamente o processo da otimização do circuito. Ao contrário de outros métodos disponíveis na literatura, o AIDA-PEx estima as capacidades e resistências de um *layout* simplificado que inclui os dispositivos e uma versão não detalhada das ligações entre eles, utilizando um método empírico suportado pelos dados retirados dos ficheiros da tecnologia. O AIDA-PEx usa os dados empíricos fornecidos juntamente com considerações geométricas para modelar os componentes parasitas num modelo 2.5-D. Os resultados experimentais são apresentados para o processo de dimensionamento da *United Microelectronics Corporations* (UMC) 0.13 μ m, e comparados com o extrator de parasitas Mentor Graphics' Calibre®, referência nesta indústria. Nestes testes, 90% das soluções obtidas com a otimização tradicional não cumpriam as especificações depois do *layout*, comprovando a importância da metodologia proposta.

Palavras-Chave

Projecto de Circuitos Integrados Analógicos

Projecto Assistido por Computadores

Automação de Projecto Eletrónico

Dimensionamento de Circuitos tendo em conta efeitos da Representação Física

Extracção de Parasitas

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Table of Contents

Abstract	i
Keywords	i
Resumo	iii
Palavras-Chave	iii
Acknowledgements	v
Table of Contents	vii
List of Tables	ix
List of Figures	xi
List of Abbreviations	xiii
Chapter 1 Introduction	1
1.1 Motivation	2
1.2 Research Goals	3
1.3 Contributions	4
1.4 Document Structure	5
Chapter 2 State-of-the-Art	7
2.1 Layout-aware Analog Synthesis	7
2.2 Parasitic Extraction	10
2.3 Standard Industry Tools	14
2.4 Conclusions	15
Chapter 3 AIDA's Synthesis Flow	17
3.1 Integration on AIDA Framework	17
3.2 AIDA-PEx Architecture	19
3.2.1 Inputs	19
3.2.2 Technology Design Kit Processing	21
3.2.3 Parasitic Extraction	21
3.2.4 Outputs	22
3.3 Conclusions	23

Chapter 4	TDK Processing.....	25
4.1	TDK tables.....	26
4.2	Preliminary tests	31
4.2.1	Case Study I: <i>Two parallel stripes of Metal (1, 4, 8)</i>	31
4.2.2	Case Study II: <i>Stripe of Metal X above a Stripe of Metal 1 (parallel)</i>	34
4.2.3	Case Study III: <i>Stripe of Metal 2 above a Stripe of Metal 1 (perpendicular)</i>	35
4.3	Conclusions	37
Chapter 5	Parasitic Extraction.....	39
5.1	Parasitic Resistance	40
5.2	Parasitic Capacitance.....	41
5.2.1	Substrate Capacitance (C_S).....	41
5.2.2	Interconnect Capacitance (C_I).....	42
5.3	Geometrical considerations	46
5.4	Preliminary Tests	47
5.5	Conclusions	48
Chapter 6	Results.....	49
6.1	Case Study I – Single Ended 2-Stage Amplifier.....	49
6.2	Case Study II – 2-Stage Folded Cascode Amplifier	53
6.3	Conclusions	55
Chapter 7	Conclusions and Future Work	57
7.1	Conclusions	57
7.2	Future Work.....	57
Chapter 8	References	59

List of Tables

Table 2-1 – Comparison between state-of-the-art works on layout-aware sizing with special detail to layout-related data.	9
Table 4-1 – Results for <i>Case Study I</i>	32
Table 4-2 – Results for parallel slide.	33
Table 4-3 – Results for perpendicular slide.	34
Table 4-4 – Results for <i>Case Study II (Part I)</i>	35
Table 4-5 – Results for <i>Case Study II (Part II)</i>	36
Table 4-6 – Results for <i>Case Study III</i>	37
Table 5-1 – Intra-module Capacitance Comparison.	48
Table 6-1 – Direct Bulk Capacitance Comparison.	50
Table 6-2 – Direct Interconnect Capacitance Comparison for 51dB Layout.	50
Table 6-3 – Direct Interconnect Capacitance Comparison for 75dB Layout.	51
Table 6-4 – Pre/Post-Layout Simulation.	51
Table 6-5 – Illustration of resulted layouts for the 51dB circuit.	52
Table 6-6 – Illustration of resulted layouts for 75dB circuit.	53
Table 6-7 – Performance Comparison for the traditional and layout-aware optimizations.	54

List of Figures

Figure 1-1 – Traditional Analog IC Design Flow.	2
Figure 1-2 – Layout-aware loop in optimization-based sizing.	3
Figure 2-1 – Electric field lines on conductors storing different charges.	11
Figure 2-2 –The various capacitances considered in 2.5-D modeling.	12
Figure 2-3 – 3-D modeling as a combination of two 2-D structures.	13
Figure 2-4 – Mentor Graphics’ Calibre® parasitic extraction GUI [4].	15
Figure 3-1 – AIDAsoft website [29].	17
Figure 3-2 – AIDA Layout-aware Environment.	18
Figure 3-3 – AIDA-PEx architecture.	20
Figure 3-4 – Router output comparison.	20
Figure 3-5 – Parasitic netlist example with π 2 model.	22
Figure 4-1 – TDK Processing architecture: Interpolation and Empirical Models.	25
Figure 4-2 – Example of a foundry table, <i>metal1</i> above <i>substrate</i> (M1/ SUB) for the UMC 130nm.	26
Figure 4-3 – 3-D representation of Area Capacitance.	27
Figure 4-4 – 3-D representation of Fringe Capacitance.	27
Figure 4-5 – 3-D representation of Coupling Capacitance.	28
Figure 4-6 – 2-D representation of Area Capacitance.	28
Figure 4-7 – Linear-by-segments interpolation of Area Capacitance.	29
Figure 4-8 – 2-D representation of Fringe Capacitance.	29
Figure 4-9 – Linear-by-segments interpolation of Fringe Capacitance.	30
Figure 4-10 – 2-D representation of Coupling Capacitance.	30

Figure 4-11 – Linear-by-segments interpolation of Coupling Capacitance	31
Figure 4-12 – Capacitances considered on <i>Case Study I</i>	32
Figure 4-13 – Geometrical parameters on parallel slide.	32
Figure 4-14 – Geometrical parameters on perpendicular slide.....	33
Figure 4-15 – Parameters took into account on <i>Case Study II</i>	35
Figure 4-16 – Parameters took into account on <i>Case Study III</i>	36
Figure 5-1 –Parasitic extractor architecture: Resistance Modeling, Capacitance Modeling, Geometrical Considerations.....	39
Figure 5-2 – Intrinsic resistance of a conductor.	40
Figure 5-3 –Parasitic wire resistance computed by square counting [3].	41
Figure 5-4 – Capacitances considered to compute substrate capacitance.	42
Figure 5-5 – Capacitances considered for interconnect capacitance on the same layer.	43
Figure 5-6 – Interconnect capacitance for overlapping plates (2D view).	44
Figure 5-7 – Interconnect capacitance for non-overlapping plates (3D view).....	44
Figure 5-8 – C_F decay with respect to the space between conductors.	44
Figure 5-9 – C_F decay with respect to the lower plate's width.	45
Figure 5-10 – Top view example of space occupation analysis.....	46
Figure 6-1 – Single ended 2-stage amplifier used as respective POF.....	49
Figure 6-2 – Traditional and Layout-aware optimization POFs (Case Study I).	52
Figure 6-3 –2-stage folded cascode amplifier.	54
Figure 6-4 – Traditional and Layout-aware optimization POFs (Case Study II).	55
Figure 6-5 –Illustration of resulted layouts (Case Study II).	55

List of Abbreviations

CAD	Computer-Aided-Design
CMOS	Complementary Metal Oxide Semiconductor
DRC	Design Rule Check
DSM	Deep-SubMicrometer
DSP	Digital Signal Processing
EDA	Electronic Design Automation
GUI	Graphical User Interface
IC	Integrated Circuit
LVS	Layout Versus Schematic
POF	Pareto Optimal Front
RF	Radio-Frequency
SoC	System-on-a-Chip
TDK	Technology Design Kit
UMC	United Microelectronics Corporations
VLSI	Very Large Scale Integration

Chapter 1 Introduction

This chapter presents a brief introduction to the traditional analog integrated circuit design flow and to electronic design automation with particular emphasis on layout-aware sizing methodologies, which are the focus of this work. Then, the motivation for this dissertation is presented, and, finally, the research goals and contributions are outlined.

In the recent past, the ever-increasing demand for microelectronic devices led to the massive improvement in the area of Very Large Scale Integration (VLSI) technologies, allowing the proliferation of consumer electronics and enabling the steady growth of the Integrated Circuits (ICs) market. The increase in IC complexity is mostly supported by an exponential growth in the density of transistors while inversely reducing the transistors' cost, which allows the designers to build multimillion transistor ICs. This increase in the design complexity is only possible to follow because IC designers are assisted by Computer Aided Design (CAD) tools that support the design process [1][2].

Most functions in today's ICs are implemented using digital or Digital Signal Processing (DSP) circuitry, and, although analog blocks constitute only a small fraction of the components on mixed-signal ICs and system-on-a-chip (SoC) designs they still play a major role. Analog ICs are known for its difficult re-utilization, so designers have been replacing analog circuit functions for digital computations, however, there are some blocks that stubbornly remain analog, e.g., sensor interfaces, sample-and-hold circuits, analog-to-digital converters and frequency synthesizers.

Unlike digital circuits, where the low-level phases of the design process are automated using fairly standard methodologies, the synthesis and layout of analog circuits is most of the time a manual task. The absence of mature design automation tools creates a great dependence on human intervention in all phases of the design process, which, despite being supported by circuit simulators, layout editing environment and verification tools, results in a time-consuming and error-prone design flow when compared to the development time of the digital blocks.

Despite the advantages that the new fabrication technologies bring to IC performance, the reduced size and high density of devices, especially in modern analog ICs, add new challenges to analog designers. The effects of non-idealities, variability of the fabrication process parameters and circuit's parasitics causes disturbances that, if not being weighted in the early stages of development, can be responsible for design errors and expensive re-design cycles, becoming the bottleneck of SoC and mixed-signal ICs design.

Traditionally, the design flow of analog ICs starts with the topology selection, where the user determines the most appropriate circuit topology in order to meet a set of given specifications.

Given a selected topology, the specifications are translated from system-level to cell-level, where the task is reduced to circuit sizing. At each specification translation step the circuit is tested and resized until all the initial specifications are met. When the obtained circuit meets the desired performance, the next task of the design flow is the layout synthesis, in which the fabrication masks that are used to produce the devices are drawn using the sizes obtained from the previous step, as illustrated in Figure 1-1.

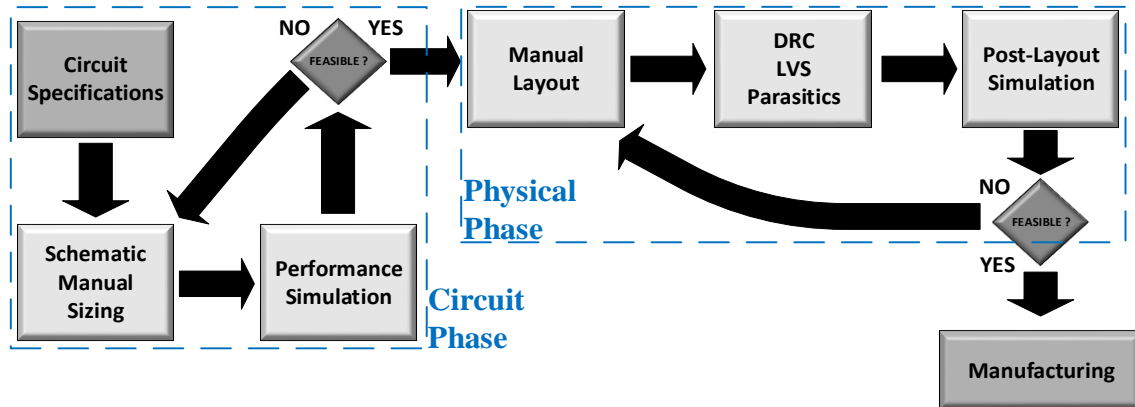


Figure 1-1 – Traditional Analog IC Design Flow.

In this traditional flow, the layout generation task is only triggered when the sizing task is complete, but in order to overcome the increasing impact of layout parasitic effects in circuit's performance, sizing and layout design phases tend to overlap with non-systematic iterations between these electrical and physical design steps. If these effects are not accounted for, the circuits' post-layout performance can be compromised, and, if the circuit is wittingly overdesigned the result is a waste in power and area. Furthermore, even the evaluation of the circuit area or aspect ratio is practically impossible from the netlist alone without any layout generation.

1.1 Motivation

In digital IC design several Electronic Design Automation (EDA) tools and design methodologies are available to help the designers keeping up with the new capabilities offered by the integration technologies, while analog design automation tools are not keeping up with the new challenges created by technological evolution. This lack of automation drives analog designers to manually explore the solution space searching for a solution that fulfills the design specification, a task that's both exhaustive and time consuming, not to mention that even if the solution is found, it rarely is the optimal solution. Optimization-based tools are of the utmost help to analog IC designers, not only accelerating the sizing process, but also providing reliable solutions.

Hence, to address post-layout performance degradation and geometric requirements earlier in

the design flow, the, so called, layout-aware or layout-driven design approaches automatically include layout effects during the automatic sizing loop, to trim down the effects of high-order non-idealities and parasitic disturbances that affect analog circuits' performance. However, to achieve post-layout successful designs that meet all specifications, time-consuming tasks like layout generation and parasitic extraction are required inside the sizing loop, as sketched in Figure 1-2. This time cost will affect the optimization loop delaying each iteration, and consequently, exponentially increasing total runtime.

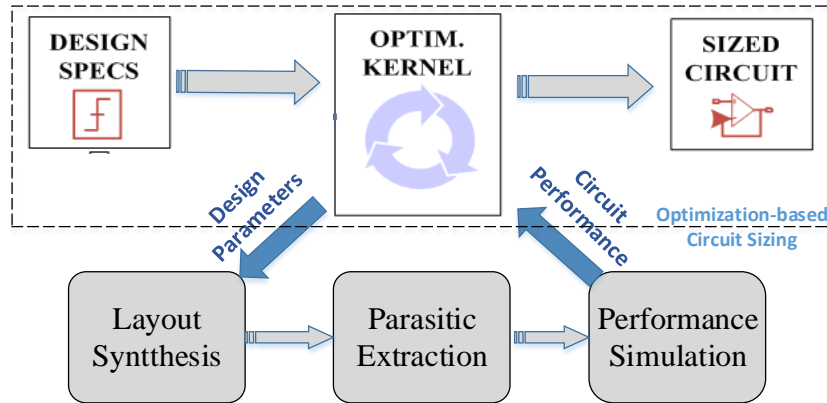


Figure 1-2 – Layout-aware loop in optimization-based sizing.

There are several existing commercial tools to accurately extract the circuit parasitics (*ANSYS Q3D*, *StarRC*, *QRC*, *Calibre*, etc.). The problem using these extractors, in the automatic sizing loop, is either the setup time required to have the entire Design Rule Check (DRC) and Layout Versus Schematic (LVS)-clean layout coded in a procedural generator, which should also be flexible to accommodate different placement and routing layouts, or the execution time required to obtain the complete full layout design using a custom generator, which is one of the most time consuming tasks on the automatic analog layout flow [3].

1.2 Research Goals

Innovative layout-aware sizing methodologies are emerging in the EDA community and represent an important part of the future of analog design automation, closing the gap between electrical and physical design for a unified sizing and layout process. Fast, flexible and complete layout generation and parasitic extraction techniques are required to promptly include layout-related data into the sizing process, however, these are usually exhaustive and time consuming tasks in both manual and automation realities. In order to overcome these problems, the automatic flow proposed in [3] shows the advantages of the layout-aware approach using a simplified layout description enhanced with quick estimates for parasitics, but the truth is that designers' trust is in the industry "standard" extraction tools.

The methodology presented in this document focuses on the parasitic extraction task of analog ICs, however, the main goal of this work is to enable the layout-aware optimization task to be more precise and robust, with a lightweight parasitic extractor that accurately estimates the effects of non-idealities in the layout and leads the optimization of the circuit. In this context, a customized tool is then of utmost relevance to a correct and fast parasitic estimation. The goals of this research can be summarized as:

- To create a fast parasitic extractor that can be embedded in a layout-aware analog IC optimization loop without compromising running time. However, in order to meet the designers' expectations, it is important to have results with high accuracy, i.e., comparable with the results of an industry-standard commercial extractor; hence it must also be accurate in estimating the values of the parasitics to properly lead the circuit's optimization.
- To determine the set of parasitic capacitances and resistances that further influence the group of studied circuits (class of analog amplifiers and similar). Experimental tests to partial layouts have been done with this purpose (layouts containing only devices, only routing paths, etc.);
- To develop a set of heuristics that are able to run accurately not only over the complete layout, but also over the incomplete layout, which has only the global routing, and is used in the optimization loop to accelerate the process. Currently, extractors integrated in layout-aware methodologies can only operate over complete layout descriptions;
- To approximate as much as possible the estimated parasitic components from the ones extracted by an off-the-shelf commercial tool. Even though the results from the developed module are extracted from an early-stage of the layout instead of the complete and detailed layout.

1.3 Contributions

The primary goals of AIDA-PEx, the proposed extractor, are to be fast and precise that can be introduced in the optimization loop with the upmost confidence. Most approaches where parasitic extraction has high accuracy require the complete full layout design with detailed routing, which is one of the most time consuming tasks on the automatic analog layout flow. Moreover, these approaches rely on procedural layout generators that lack on flexibility to handle specification or topological changes. In order to accelerate in-loop process, AIDA generates a simplified routing that only sketches the routing paths in *metal1* stripes and extracts the parasitic layout components from them. Therefore, a major contribution of AIDA-PEx is

being able to work over a complete detailed layout as well as over the simplistic layout generated in the optimization loop.

AIDA-PEX was tested and validated with a set of operational amplifier circuits for the UMC 0.13 μ m process and compared with the industry standard Mentor Graphics' Calibre®, ensuring high accuracy even when running over the simplified layout, used in the optimization loop. By considering new accurate models for the technology dependent parameters, a new computation of substrate and interconnect capacitance and new geometrical considerations, a complete parasitic extractor is implemented that guarantees fast and solid results.

These characteristics empower the optimization process when AIDA-PEX is integrated in the loop, allowing the performance measurements to be more realistic and precise. The layout-aware sizing task culminates in optimal and robust solutions. The promising achieved results led to a paper submission:

- B. Cardoso, R. Martins, N. Lourenço and N. Horta, "AIDA-PEX: Accurate Parasitic Extraction for Layout-Aware Analog Integrated Circuit Sizing," in *IEEE PhD Research in Microelectronics and Electronics (PRIME)*, Glasgow, Scotland, July 2015 (Submitted on March 2015).

1.4 Document Structure

The rest of this document is organized as follows:

- Chapter 2 presents an overview of the state-of-the-art in layout-aware analog integrated circuit sizing, focusing on the layout generation approaches and parasitic extraction methods that are used.
- Chapter 3 sketches the flow of AIDA, specifying the different tasks of each module. It also presents a brief introduction to AIDA-PEX architecture.
- Chapter 4 describes the empirical data used to compute the parasitic components, illustrating the variation of the values according to the look-up variables and explaining the chosen regression.
- Chapter 5 details the approach chosen to create the extractor, showing the different considerations that led to the modeling, computation and approximation of the estimated capacitances.
- Chapter 6 presents some case studies to test the parasitic extraction and consequent extracted netlist performance simulation. The results are compared with Mentor Graphics' Calibre® [4].
- Chapter 7 addresses the closing remarks and some directions for future developments are suggested.

This chapter starts by addressing the state-of-the-art in Layout-Aware Analog Synthesis and in the second section an overview of the past works and approaches on accurate/fast parasitic extraction is presented.

2.1 Layout-aware Analog Synthesis

In the past few years, several tools that implement a layout-aware analog synthesis of ICs have emerged. Yet, in most of them the process is not completely automatic, with various phases still requiring user input and handmade design, either on circuit sizing or layout generation.

The behavior of analog circuits is extremely sensitive to layout-induced parasitics. Parasitics not only influence the circuit performance but often render it non-functional. Hence, it is essential to consider the effect of parasitics early in the design process. Traditionally, the circuit synthesis step is followed by layout synthesis and each step is carried out independent of the other. This is followed by a verification step to check whether the desired performance goals have been achieved after layout generation and extraction. These steps are carried out iteratively until the desired performance goals are met. This approach is extremely time-consuming and no structured feedback from previous runs can be readily used to re-design the circuit if the layout fails to meet performance goals. One way of performing layout-aware synthesis is to perform layout synthesis and extraction inside the circuit synthesis loop, so fast procedural layout generators are generally used.

Vancoreland et al. [5] uses genetic algorithms with manually derived performance models to evaluate the circuit parameters. Integrated in the loop, the layout is created with a procedural generator and geometric data is obtained with sculptured equations. Fitted functions are used to test the performance of the circuit and the data related to the parasitics of the layout is extracted by a 1-D/2-D modeling but only applied for the area and fringing capacitance of the metal1 and poly stripes of the circuit's critical nets.

Ranjan et al. [6] uses pre-compiled symbolic performance models to evaluate the circuit's performance at each iteration of the loop, thus avoiding numerical simulation. To this models are passed the area and interconnect parasitic values along with the passive component values. The layout is rapidly created with a parameterized procedural generator which consists on a fixed template layout, which serves as a blueprint to the mapping of the components, which are instantiated when the parameters of the circuit are given. The circuit's parasitics are obtained using an external extractor.

Pradhan et al. [7] starts by sampling a design space to generate circuit matrix models that can

predict the circuit performance at each iteration. For a uniform number of design points, a procedural generator creates layout samples (it doesn't actually generate the complete layout in-loop to reduce iteration time), and bulk, device and interconnect parasitics are modeled by linear regression. With the goal of optimizing conflicting performance objectives, it creates a Pareto-optimal surface with points spread uniformly in all regions.

Youssef et al. [8] implements a simulation-based circuit synthesizer. A Python-based procedural layout generator ensures different layout styles for the same analog blocks, opening the results to some variation on the optimization variables. The layout-related data addressed by the generation tool includes modeling of the stress effects of the devices and some geometrical measures, using analytical models to obtain the values for the circuit's parasitics.

Habal et al. [9] uses a deterministic placer where every possible layout for each device in the circuit is generated and investigated using a placement algorithm Plantage [10]. The layouts with undesirable geometric features are then discarded and only the final selected placement based on area, electrical performance and aspect ratio is routed. Designer knowledge is supplied by geometric circuit placement and routing constraints, then a deterministic nonlinear optimization algorithm is used for circuit sizing. A complete extraction of circuit's parasitics is made using Cadence Assura®.

Castro-Lopez et al. [11][12] deals with both parasitic-aware and geometrically constrained sizing, creating new optimization variables which can therefore include solutions for optimized area and shape of the total circuit. Using commercially available tools to evaluate the performance of the circuit, it attains highly integrated solutions by creating a coded slicing-tree to generate a predefined template. The templates implemented by using the Cadence pCells technology and SKILL programming avoid long iteration times. Without actually generating the layout, 3-D parasitic estimation was achieved with template sampling techniques and analytical equations.

Liao et al. [13] implements a user assisted tool, where designer decision and knowledge is inputted during circuit sizing and layout template configuration. The program uses analytical models for the layout-related data, where polynomial equations derive the values of the capacitances from geometrical data, from the layout template, and technology parameters.

A synopsis of all these works is presented in Table 2-1, with special attention to the provided layout-related data.

Table 2-1 – Comparison between state-of-the-art works on layout-aware sizing with special detail to layout-related data.

Work	Circuit Synthesizer	Performance Evaluation	Layout Generator		Layout-related Data						Observations
			Placer	Router	Geometric	Parasitics Included				Resistances	
						Bulk	Intra-Device	Inter-Device	Routing Wires		
Vancorenland et al. [5]	Performance models and Genetic algorithms	Fitted functions	Procedural generator		Equations	✗	✓	✗	✓	Gate	1/2-D analytical-geometrical modeling of the critical nets
Ranjan et al. [6]	Optimization-based	Symbolic models	Procedural generator (design space sampled)		No	✗	✓	✓	✓	✓	Area and interconnect using external extractor
Pradhan et al. [7]	Multi-objective Opt.	Symbolic models	Procedural generator (design space sampled)		No	✓	✓	✗	✗	✗	Analytical models for bulk, device and interconnect
Youssef et al. [8]	Simulation-based Opt.	Circuit simulation and Design plans	Procedural generator		Yes	✓	✓	✗	✗	✗	Modeling of the stress effects of the devices
Habal et al. [9]	Simulation-based Deterministic nonlinear	Circuit simulation	Enumeration of all possible floorplans	Exhaustive setup for Cadence Chip Assembly Router®	Yes	✓	✓	✓	✓	✓	Complete extraction using Cadence Assura®
Lopez et al. [11][12]	Simulation-based Multi-objective Opt.	Simulation (Spectre® or HSPICE®)	Coded Slicing-tree	Template-based	Yes	✓	✓	✓	✓	✗	3-D analytical-geometrical
Liao et al. [13]	User Assisted				Yes	✗	✓	✓	✓	✓	Analytical models for area and interconnect
This work, AIDA	Simulation-based Multi-objective Opt.	Worst case corner simulation (Spectre®, Eldo® or HSPICE®)	Multiple B*-trees	Automatic electromigration-aware wiring topology and global routing in-loop	Yes	✓	✓	✓	✓	✓	2.5-D modeling of the devices and routing that operates over non-detailed routing

In [5][6][7][8] procedural generators are used (in-loop or for layout sampling), on which the whole layout of the circuit is coded and require huge setup times. Furthermore, these don't support wide specification changes, and, if any topology or technology changes are necessary a complete setup/re-design of the circuit is inevitable.

In [11][12] the flexibility of the layout generator is improved by the use of a template-based approach supported on a slicing model, but due to the multitude of different sizing solutions found throughout the whole Pareto solution set it is almost impossible to pack all the solutions properly with the same fixed template. The alternative presented in [9] is fully automatic generation with an exhaustive search, but costing the increase in computation time. However, for all approaches, routing template is the same for all design solutions and is not fitted to the solutions as they vary in a multitude of devices' sizes/shapes and performances.

In [5] a 1/2-D analytical-geometrical model was chosen for parasitic estimation, but it is only applied for the area and fringing capacitance of the *metal1* and *poly* stripes of the circuit's critical net(s), which makes the estimation quick, but loses accuracy and needs user intervention to identify the critical net(s). This can lead to errors, if, depending on layout, less critical nets became problematic.

In [7][11][12][13] analytical polynomial models with predictor variables, such as diffusion area/perimeter or even voltages/ currents from circuit simulation are used, yielding a very fast estimation of the parasitic impact on circuit's performance without post-layout simulation. Still these values are just predictions and can have a large error. In [8] analytical models are also used, but the predictor variables related to the transistors' stress effects, which are distances between components, do require some post-layout analysis.

In [6][9] an external extractor is used which guarantees accurate results for the parasitic estimation. Although the parasitics obtained by using these techniques are very accurate, their inclusion in the optimization loop either forces the creation of a custom parameterized layout, which adds considerable setup time, or using custom full layout generator, which is prohibitively slow to use inside the optimization loop.

2.2 Parasitic Extraction

Parasitic effects are becoming more critical with the increase in performance, density, complexity and levels of integration in deep-submicrometer (DSM) designs. In IC design, the final area occupied by the elements of the circuit is often one of the optimization variables, which every designer wants to minimize. With that in mind, designers place the components as closer as they can, following the DRC rules, leading to very compact floorplans. In this subsection the main works on parasitic extraction are outlined and analyzed.

A parasitic element arises due to the proximity of conductors or the lengths of traces, wires, or leads of components, because when two conductors at different potentials are close to one another, they are affected by each other's electric field and store opposite electric charges, forming a capacitor, as illustrated in Figure 2-1.

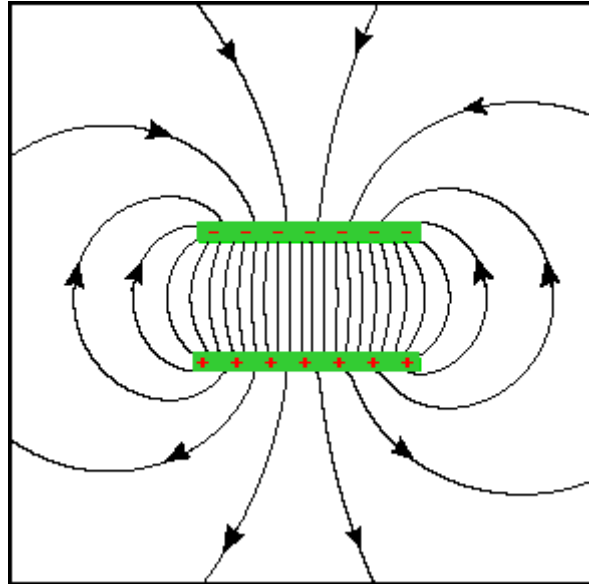


Figure 2-1 – Electric field lines on conductors storing different charges.

A conductor (or terminal) has an intrinsic capacitance relative to the substrate and an interconnect capacitance concerning each one of the nearby conductors. Depending on the relative positioning of the conductors at issue, many situations can arise, leading to different classifications to the existing capacitances.

There are three primitive capacitance classifications: Area Capacitance (C_A), Fringe Capacitance (C_F) and Coupling Capacitance (C_C), as illustrated in Figure 2-2. Coupling capacitance is only present when the evaluation is being conducted between conductors in the same layer. Area capacitance is only present when two conductors in different layers overlap, corresponding to the field lines existent in the area on which these conductors overlap. Fringe capacitance refers to the rest of the lines that curve around the conductors. With an important role in parasitic estimation, fringe capacitance is the hardest to understand and estimate, due to the geometrical implications it requires.

Even though the latest processing technology advancements on lowering the relative constant of the dielectric reduce the effect of the parasitic capacitances, the continued scaling down of the feature size keeps the parasitic effects dominant. The capacitance extraction advanced from 1-D, 2-D, quasi-3-D (or 2.5-D) to 3-D effects to meet the required accuracy.

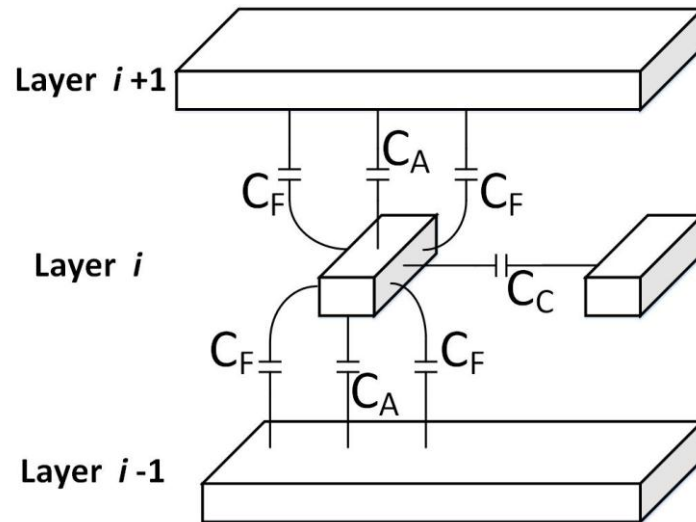


Figure 2-2 –The various capacitances considered in 2.5-D modeling.

In the first approaches a 1-D capacitance extraction was used, which calculates the values by weighting the area and perimeter of interconnect geometries into an expression (only C_A component). Then, 2-D extraction was introduced where the parameters set is extended to account for the same layer capacitive effect. In other words, not only conductor's overlap C_A is addressed but also the effect two conductors in the same layer have on each other, i.e., C_C component.

Still, the 2-D approaches doesn't cover the effect of 3-D structures such as two wires crossing, so a 3-D pattern is needed to address the non-overlapping capacitance between interconnects of different layers. However, there are numerous variations in 3-D structures and 3-D capacitance extractors are not trivial extensions of 2-D ones.

An extension to address 3-D effects is the 2.5-D method, where the 3-D effect is modeled as a combination of two orthogonal 2-D structures [14], as it is illustrated in Figure 2-3. By carefully composing a 3-D solution from the two orthogonal 2-D ones, most 3-D effects are captured, avoiding the complicated 3-D evaluation.

The 3-D modeling is always complicated due to the geometrical implications it requires. From the basic capacitances used to compute the more complex ones, only fringe capacitance is challenging to modulate precisely because of the geometrical considerations needed to correctly estimate the values. The area and coupling capacitance have well defined areas of effect, but for fringe capacitance this area is not so well delimited.

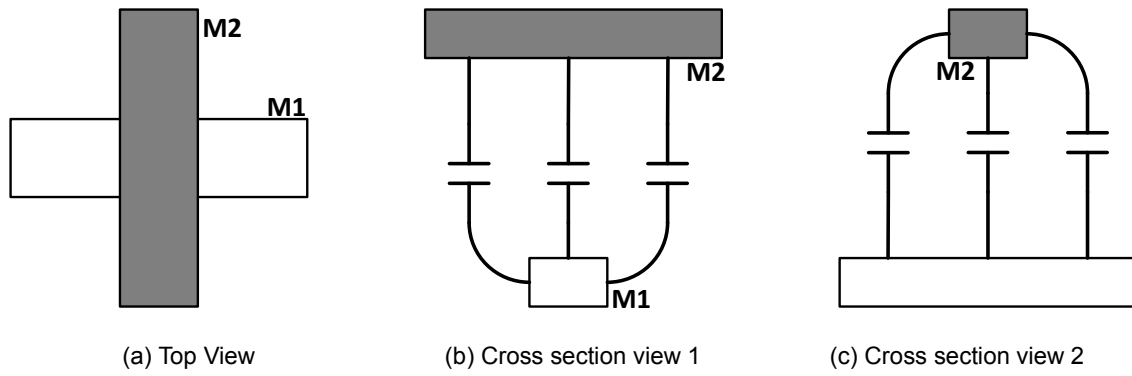


Figure 2-3 – 3-D modeling as a combination of two 2-D structures.

In past years, many works on accurately modulating the fringe capacitance were developed. Bansal et al. [15] proposed an analytical model to compute the fringe capacitance between two non-overlapping interconnects in different layers using a conformal mapping technique. These models are derived by analyzing the electrostatics between interconnects and using technology-dependent parameters. The conformal mapping technique replicates the characteristics of the electrical field lines between conductors to modulate the effect of fringe capacitance.

More recently, Shomalnasab et al. [16] took this idea to modulate fringe capacitance based on electric flux and applied it on interconnect estimation, in the same layer or in different layers. In this technique, massive geometrical considerations are needed along with technology dependent data. First, a general template for the fringe capacitance based on fundamental electromagnetic principals is derived, and then, the accuracy is improved with a fitting technique.

Following the analytical approach, Sharma et al. [17] presented closed-form analytical expressions for interconnect parasitic capacitances in VLSI, derived from variation analysis. Although analytical models can be very accurate, the implications they would bring for more complex modules (common centroid, etc.) and the difficulty of deriving the technology related parameters, make the use of these techniques inside an optimization loop impracticable.

There are a few works that, trying to accelerate the process, estimate the different capacitances even before complete layout generation. Yu et al. [18] created a 2-D pattern characterization for pre-route stage, with a pattern-library method. Then circuit's congestion is estimated and linear interpolation is carried over a conductors' width variable. In this work, resistances are calculated with analytical equations. Trying to estimate the values for the capacitances even earlier, Foo et al. [19] derives parasitics evaluating floorplan density. A look-up table is then created mapping each density reading to an appropriate spacing value.

Vemuri et al. [20][21] was the first to study parasitic extraction with the purpose of embedding it

in a layout-aware sizing approach, not only regarding the resulted accuracy, but also the extraction runtime. This work uses an empirical method, where massive look-up tables are accessed to estimate the parasitic components. Additionally, the data is processed with determinant decision and multi-variable linear interpolation. This approach might not achieve such higher levels of accuracy but it is a fast method for parasitic component estimation.

In order to achieve ultimate levels of accuracy, Karsilayan et al. [22] calibrates a set of various analytical equations based on layout parameters. Additionally, a field solver is used, which is a specialized program to directly solve a subset of Maxwell's equations [23]. The 2-D field solver provides capacitance and sensitivity data to fit the layout parameters to the analytical formulas, resulting in a 2.5-D parasitic extraction framework.

This work was applied in Mentor Graphics' Calibre®, which is one of the available industry tools for parasitic extraction in the market. In the next subsection, the off-the-shelf parasitic extraction/estimation tools are outlined.

2.3 Standard Industry Tools

In the recent past years, several commercial tools have emerged in the analog layout EDA market to estimate parasitics, and even though the methods and formulations they implement are still secret for business reasons, some brief specifications are presented next:

- **ANSYS Q3D Extractor [24]:** uses a method of moments (integral equations) to compute capacitive, conductance, inductance and resistance matrices.
- **FastCap, FastHenry [25]:** from *MIT* (Massachusetts Institute of Technology) are two free parasitic extractor tools for capacitance, inductance and resistance. Quoted in many scientific articles, are considered golden references in the field.
- **StarRC [26]:** from *Synopsys* (previously from *Avanti*) is a universal parasitic extractor tool applicable for a full range of electronic designs. It uses a 3D field solver for the critical nets of circuits.
- **Assura QRC [27]:** is the parasitic extractor tool from *Cadence* for both digital and analog designs. It is integrated with the leading transistor-based parasitic extraction flow.
- **Calibre xACT 3D [4]:** from *Mentor Graphics* is, unlike other tools, a 3D field solver modeling engine built on advanced software algorithms to accurately calculate parasitic effects at the transistor level. It accelerates the performance on a multi-CPU platform and provides much higher accuracy.

- **EMCoS PCB VLab [28]:** from *EMCoS* includes *RapidRLC* solver, which calculates resistance, inductance and capacitance matrices for complex 3D geometries.

The industry parasitic extractors that are proud to provide the highest accuracies in the market use field solvers, calculating electromagnetic parameters by directly solving Maxwell's equations. The problem with the field solvers is the high calculation burden, which makes it applicable only to very small designs or to parts of the designs. The application of these solvers to more complex layouts would exponentially increase the total extraction time, making it impracticable.

From the presented industry tools to extract parasitic elements, Mentor Graphics' Calibre® is one of the most trusted by analog designers, providing a level of accuracy that gives the designers the confidence to define it as a role model for parasitic extractors. The graphical user interface (GUI) of Calibre® is presented in Figure 2-4.

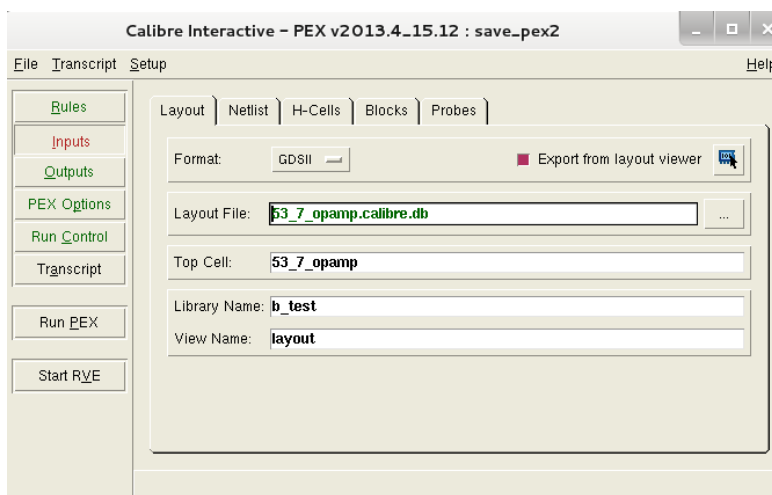


Figure 2-4 – Mentor Graphics' Calibre® parasitic extraction GUI [4].

2.4 Conclusions

In this chapter a set of tools applied to analog IC design automation were presented, with special emphasis on the parasitic extraction task, to provide a better understanding of its advantages and shortcomings. Although much has been accomplished in automatic design of analog circuits, the fact is that automatic custom generators usable in industrial design environment are just starting to gain ground.

Furthermore, layout-aware sizing methodologies are spreading and represent an important part of the future of analog design automation, closing the gap between electrical and physical design for a unified synthesis process. Beyond the efforts made towards the implementation of a layout driven optimization tool, most of the reviewed layout-aware approaches either rely on

procedural layout generations, which are known for their difficult reuse and lack of flexibility, or have massive computational times required to complete the automatic flow.

The layout-related data provided to the optimization kernel used to classify the different layouts includes the parasitic effects extracted during layout generation. The parasitic extractors used in these layout-aware approaches show that there is still a lack of quality and promptitude in the information provided. The truth is that designers still trust on standard industry tools, for the accuracy they supply. For that reason, AIDA-PEx's results are compared in the next chapters directly with the results extracted from Mentor Graphics Calibre® tool.

Chapter 3 AIDA's Synthesis Flow

This chapter first describes the process flow of AIDA, the tool on which the proposed parasitic extractor module of this dissertation is embedded, and then, the architecture of the developed parasitic extractor is presented.

3.1 Integration on AIDA Framework

The analog IC design automation framework, AIDA, on which this work was developed, implements an automatic design flow from circuit-level specification to physical layout description. AIDA results from the integration of two major analog IC design automation tools: AIDA-C, which takes care of the circuit-level sizing specification, and AIDA-L, that handles the physical layout generation. This software has its own website [29] as presented in Figure 3-1.

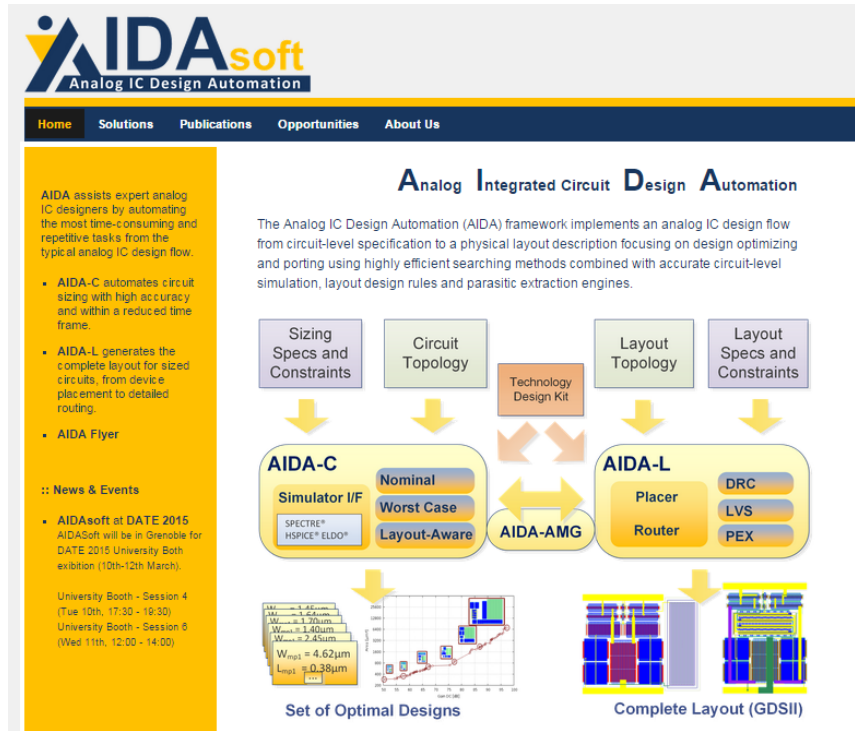


Figure 3-1 – AIDAsoft website [29].

The optimization-based circuit-level sizing is carried by AIDA-C [31], where the circuit's performance is measured using the electrical circuit simulators Spectre®, Eldo® or HSPICE®, taking into account corner analysis to ensure the robustness of the solutions. AIDA-C is based on multi-objective evolutionary optimization kernels where the inputs required from the designer are the circuit and testbench(es) netlist(s), along with the design variables and specifications. The output, instead of a single sizing solution, is a Pareto optimal front (POF) with a family of

circuits that fulfill all the specifications and represent the feasible tradeoffs between the various optimization objectives.

The layout generation is handled by AIDA-L [32], which generates the layout for each sizing solution provided. The inputs are the floorplan constraints and the set of electric-currents for each terminal, specific for each sizing solution, obtained with AIDA-C. It features a Placer, that generates a set of floorplans based on leveled templates, and a Router, which can produce a simplistic global routing or a complete detailed routing depending on the situation.

AIDA's original flow evolved to cover layout-aware sizing, where AIDA-C interacts with AIDA-L to enable the inclusion of layout-related data in the circuit synthesis task. The complete design flow is sketched on Figure 3-2.

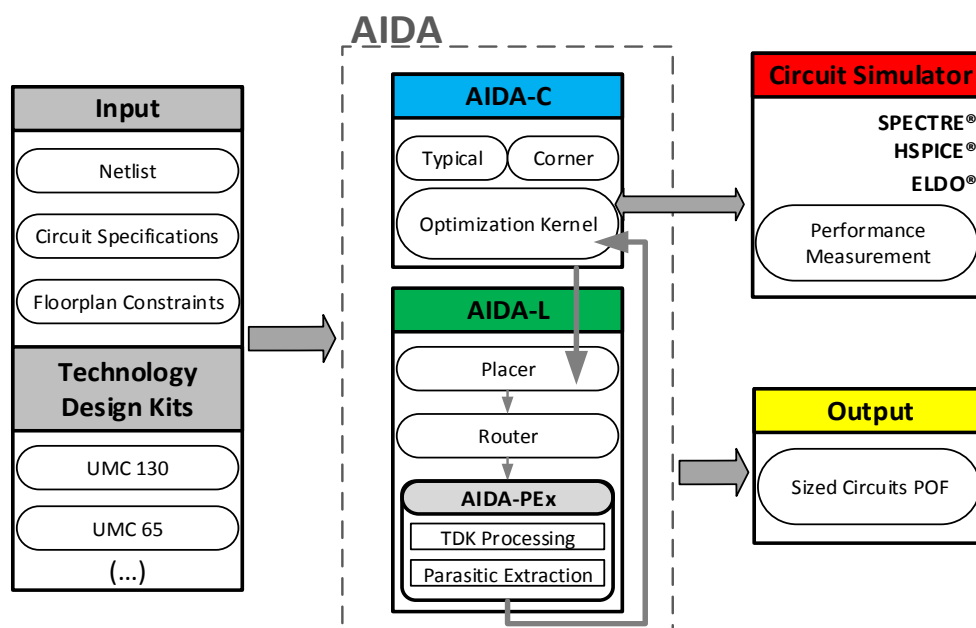


Figure 3-2 – AIDA Layout-aware Environment.

Following the loop of the optimization process, AIDA-C starts by selecting different sizing solutions, each one with a new set of design variables (e.g., devices' widths, lengths, number of fingers, etc.). Then, for each sizing solution, the DC constraints are measured using the electrical simulator, and also, the DC electric-currents for each terminal are obtained. If a solution is unfeasible (i.e., a DC constraint violated) the layout-related data is not considered for further optimization, otherwise, the solution is provided to AIDA-L, that generates the floorplans using a multi-template constraint-based Placer. The one that suits better the geometrical requirements is provided to the Router, where an electromigration-aware wiring topology and global routing is devised for each sizing.

After this, a built-in PEx module rapidly extracts parasitics from the global router, which is basically a path-finding algorithm that transforms terminal-to-terminal connections into rectilinear paths, without considering path overlap or design rule errors, and, back annotates them in the different netlists.

Finally, parasitic-aware performances are measured from the complete set of testbenches (DC, AC, TRAN, etc.) using the electrical simulator for all defined PVT corners and used together with the accurate geometrical properties of the circuit, measured by the Placer, in the optimization process. Given the multi-objective optimization performed in AIDA-C, the output of AIDA is a family of Pareto non-dominated layout-aware sized circuits that meet all the constraints in the presence of layout parasitics and geometrical requirements, representing feasible tradeoffs between the different optimization objectives.

3.2 AIDA-PEx Architecture

The parasitic extractor previously included in AIDA's framework uses an empirical-based technique where the technology-dependent parameters are obtained for the closest match from the experimental data provided by the foundry for a particular technology. Since this extractor finds the best match for the look-up variable in the table to extract the capacitance, a considerable error is often within this value. Moreover, very basic geometrical considerations are made, and the result is a naive extraction of circuits' parasitics.

The enhanced AIDA-PEx implements a new regression of the data proved by the technology kit, applies a more realistic capacitance and resistance modeling, and also, introduces a greater set of geometrical factors into the estimation task. A sketch of the architecture of the proposed module is presented in Figure 3-3. Although this architecture is detailed in the next chapters, a brief introduction to each task performed is presented in the next sub-sections, with special attention to the difference between global and detailed routing.

3.2.1 Inputs

The Placer embedded in AIDA-L creates a floorplan of the circuit's devices, which is then sent to the extractor. This floorplan contains the various shapes in the different layers that compose the terminals of the devices (simple transistors, common centroid, interdigitated...). These shapes are organized by net and by layer (*poly*, *metal1*, etc.) to be accessed and evaluated. After the parasitic estimation the capacitances and resistances are clustered into the respective terminals into a list, which is outputted to the netlist processor.

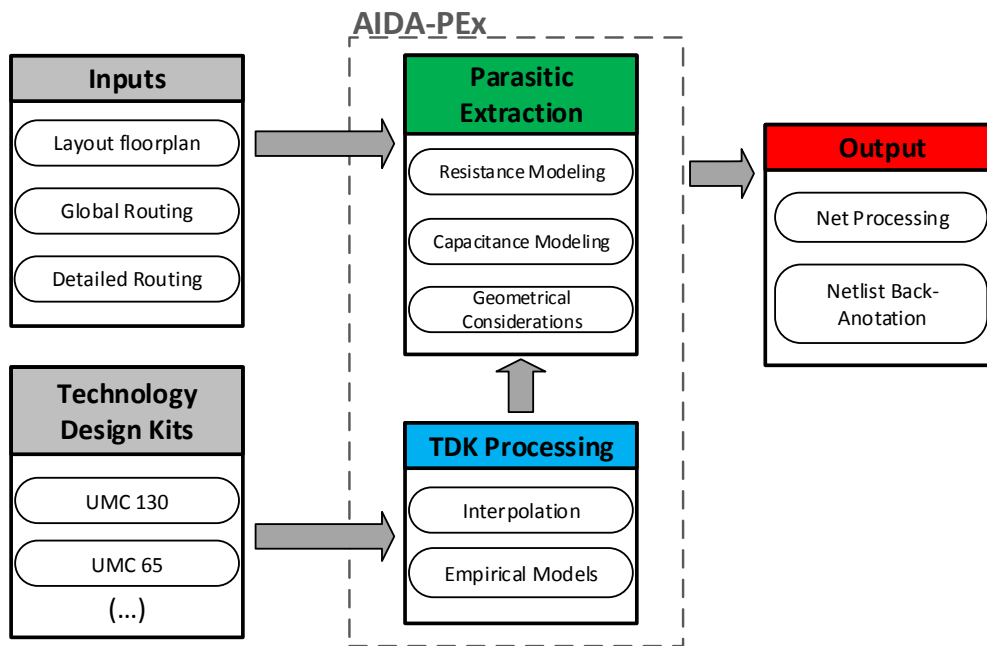


Figure 3-3 – AIDA-PEx architecture.

3.2.1.1 Detailed Routing vs Global Routing

In design automation tools the Router is divided in three parts: wiring planning, global routing and detailed routing. The wiring planner creates a connection tree, from a netlist and a set of currents, providing the optimal terminal-to-terminal connectivity while minimizing the wiring area. Then, either a global routing or a detailed one is generated and provided to the PEx module, where the parasitic estimation has to work over both of them. In Figure 3-4 a layout example of a 2-stage amplifier with both global and detailed routing is presented for comparison purposes.

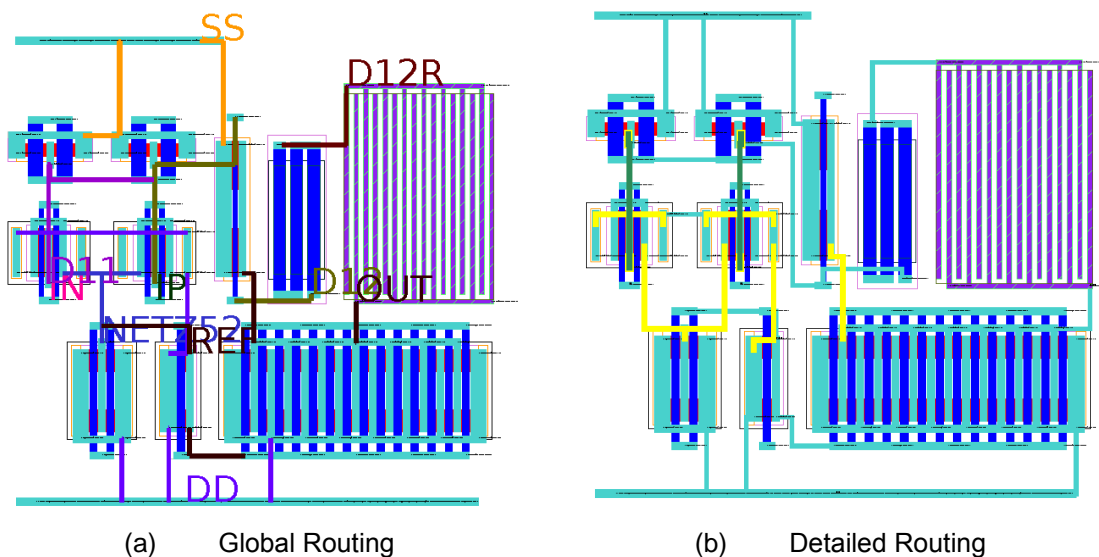


Figure 3-4 – Router output comparison.

As it is observable in the figures, the devices are placed in the same disposition in both layouts and only the routing wires are different. The detailed routing is a complete wiring of the circuits nets, checking design-rule-check (DRC) and layout-versus-schematic (LVS) tests, and the result is a correct physical layout representation of the circuit. What the global router does is outline the routing paths in *metal1* plates, without concerning DRC errors or wire overlap. The result is obviously an incorrect layout but the reason this routing is so important is the possibility of integration of this method in a layout-aware approach. The global routing procedure is a fast representation of the circuit's wiring that gives an idea of what the final routing will be, unlike the detailed routing which is a slow and tiresome procedure to ensure that the final layout is flawless. The usage of the detailed routing on the optimization loop would compromise runtime and so the need for a simplistic representation of the wiring of the circuit led to the usage of an early stage of routing.

3.2.2 Technology Design Kit Processing

The foundry data from the technology design kit considered gives standard values for certain capacitances in certain situations. This data is organized in tables, each one referring to a pair of layers. There are tables for typical, minimum and maximum values and in those tables it can be extracted area (C_A), fringe (C_F) and coupling capacitance (C_C) referent to a value of width and a value of space. A more detailed description of this data is presented on Chapter 4.

3.2.3 Parasitic Extraction

The technology foundry data is processed and modulated offline, and the respective formulas are ready to be accessed by the parasitic extraction module when needed. The desired value for the different capacitances is retreated from the TDK Processing with the respective look-up variable depending on the situation.

The parasitic extractor does five separated evaluations. First, the floorplan terminals are analyzed one by one to extract the substrate capacitance. At the same time the resistances for the various shapes of the terminals are weighted. Next, the module does the same thing for the routing wires from the global router to complete the substrate capacitance and resistance calculation.

Then three more tests are conducted to extract the interconnect capacitance amongst terminals, amongst routing paths and between terminals and wires. After the parasitic estimation, lists are created where the different capacitances are concatenated to correspond to their terminal/wire and the lists are outputted. A more detailed description of the extraction of resistances, capacitances and their geometrical considerations is presented in Chapter 5 (Sections 5.1, 5.2 and 5.3, respectively).

3.2.4 Outputs

When the parasitic extraction is complete the data is organized in lists, as referred before, and provided to the output processor, that organizes the data to be annotated in the new netlist. The parasitic estimation can be set to consider all the parasitic components or to discard the resistances, which obliges the netlist processor to have two distinct methods of annotation.

If only capacitances are considered the annotation is trivial, with the bulk capacitances being put between the node and ground, and the interconnect capacitances between the respective nodes. If resistances have to be annotated too, the annotation system is more complex. In this case the π 2 model is used (Figure 3-5(a)) where the capacitance and resistance of a net are chopped down, to ensure the effects are uniform. In Figure 3-5 an example of a wire topology for a certain net is presented and the respective parasitic netlist is illustrated.

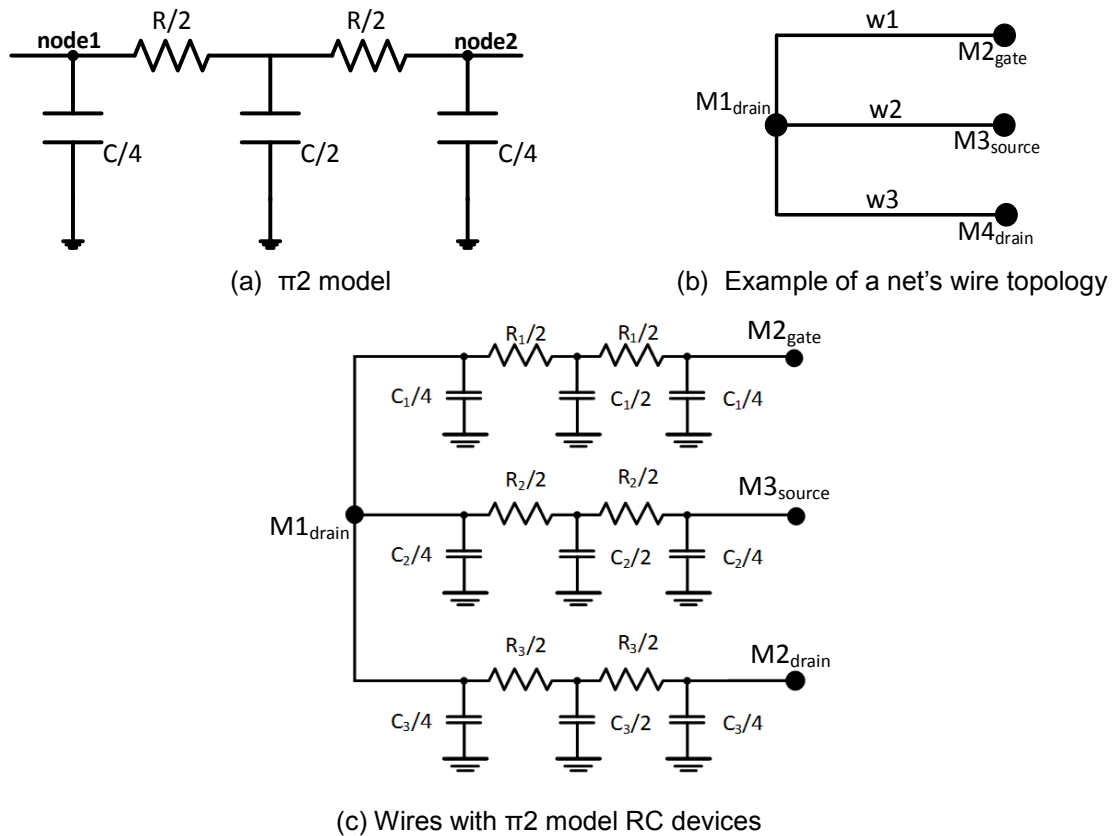


Figure 3-5 – Parasitic netlist example with π 2 model.

Here the wires are replaced by the separated components of the model to replicate the parasitic effects in the net. The new parasitic-aware netlist is then sent to the circuit simulator to measure the performance.

3.3 Conclusions

In this chapter the synthesis flow for AIDA layout-aware was described and an introduction to the parasitic extraction module was presented. Furthermore, the inputs and output were extensively specified and illustrated. In the next chapter, the AIDA-PEx module is further described and explained.

Chapter 4 TDK Processing

In this chapter, the technology design kit files are illustrated, and then, the chosen regression method to process the data is explained and tested.

The approach chosen for the parasitic extractor is an empirical-based technique where the capacitances are computed using the data existent in the foundry tables. This data needs some further processing to ensure the minimum addition of error during the process. The proposed architecture/design flow is shown in Figure 4-1, which depicts the main tasks performed.

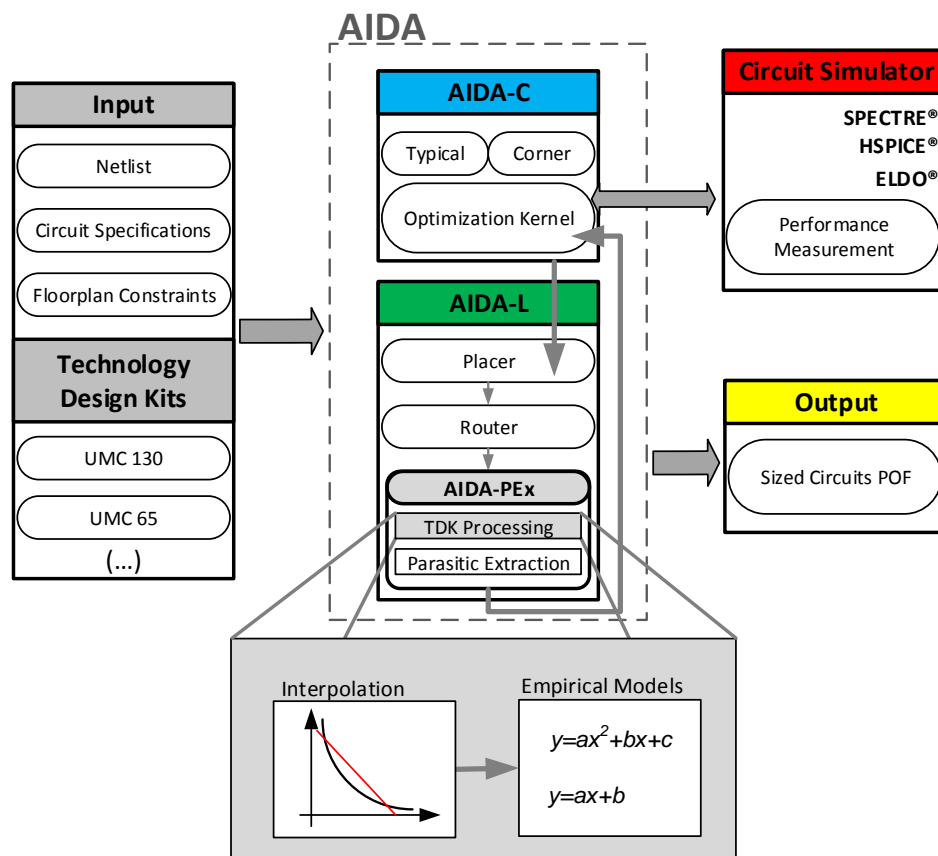


Figure 4-1 – TDK Processing architecture: Interpolation and Empirical Models.

In the next subsection (4.1), the technology design kit tables are illustrated and numerically detailed, where the graphical representation explains the chosen regression for the data. In the second subsection (4.2), some preliminary tests are conducted to understand the capacitance variation in Calibre®. In the first case study the interpolation is even tested to evaluate the associated errors, conducting a comparison between the linear interpolation used in the old version of the parasitic extractor and the linear-by-segments interpolation chosen for the new parasitic extractor. In the other case studies only the results from Calibre® are presented since it is impossible to directly compare the results to the extracted data without further geometrical

factors.

4.1 TDK tables

The approach chosen is an empirical-based technique where the capacitances are computed using the data existent in the foundry tables, one for each pair of stripes, as illustrated in Figure 4-2 for the UMC 130nm. From these PDK's, C_A (area capacitance), C_F (fringe capacitance) and C_C (coupling capacitance) can be retreated according to values of width and space.

cap	P1	SUB	480	6320	4.9785E-05	5.0230E-05	8.0689E-06
cap	P1	SUB	480	13120	4.9785E-05	5.0964E-05	2.5472E-07
# [metal1,above,substrate](typical)							
# layer1 layer2 width(nm) space(nm) C_A (fF/nm) C_F (fF/nm) C_C (fF/nm)							
#							
cap	M1	SUB	160	160	9.1808E-06	5.5824E-06	1.4383E-04
cap	M1	SUB	160	320	9.1351E-06	9.2514E-06	7.1933E-05
cap	M1	SUB	160	480	8.8154E-06	1.2703E-05	4.8790E-05
cap	M1	SUB	160	640	8.8154E-06	1.5655E-05	3.7422E-05
cap	M1	SUB	160	800	8.8154E-06	1.8289E-05	3.0189E-05
cap	M1	SUB	160	3040	8.8154E-06	3.5084E-05	5.6339E-06
cap	M1	SUB	160	4640	8.8154E-06	3.8125E-05	2.8420E-06
cap	M1	SUB	160	6240	8.8154E-06	3.9430E-05	1.7386E-06
cap	M1	SUB	320	160	1.3520E-05	7.1696E-06	1.0559E-04
cap	M1	SUB	320	320	1.4662E-05	1.0173E-05	6.8851E-05
cap	M1	SUB	320	480	1.4662E-05	1.3409E-05	4.9321E-05
cap	M1	SUB	320	640	1.4662E-05	1.6315E-05	3.8430E-05
cap	M1	SUB	320	880	1.4662E-05	2.0116E-05	2.8531E-05
cap	M1	SUB	320	1120	1.4662E-05	2.3311E-05	2.2303E-05
cap	M1	SUB	320	4480	1.4662E-05	3.8996E-05	3.3547E-06
cap	M1	SUB	320	9280	1.4662E-05	4.1771E-05	1.0283E-06
cap	M1	SUB	480	160	2.0463E-05	7.4661E-06	1.0698E-04
cap	M1	SUB	480	320	2.1970E-05	1.0271E-05	7.2525E-05
cap	M1	SUB	480	480	2.1970E-05	1.3485E-05	5.2244E-05
cap	M1	SUB	480	640	2.1970E-05	1.6394E-05	4.0874E-05
cap	M1	SUB	480	800	2.1970E-05	1.9025E-05	3.3425E-05
cap	M1	SUB	480	1440	2.1970E-05	2.7039E-05	1.8232E-05
cap	M1	SUB	480	5920	2.1970E-05	4.1465E-05	2.4235E-06
cap	M1	SUB	480	12320	2.1970E-05	4.3545E-05	7.4536E-07
cap	M1	SUB	640	160	2.7771E-05	7.5750E-06	1.1037E-04
cap	M1	SUB	640	320	2.9278E-05	1.0357E-05	7.5209E-05
cap	M1	SUB	640	480	2.9278E-05	1.3549E-05	5.4452E-05
cap	M1	SUB	640	640	2.9278E-05	1.6461E-05	4.2816E-05
cap	M1	SUB	640	960	2.9278E-05	2.1448E-05	2.9560E-05
cap	M1	SUB	640	1760	2.9278E-05	3.0101E-05	1.5370E-05
cap	M1	SUB	640	7360	2.9278E-05	4.3215E-05	1.9118E-06
cap	M1	SUB	640	15360	2.9278E-05	4.4902E-05	5.8755E-07
# [metal2,above,substrate](typical)							
# layer1 layer2 width(nm) space(nm) C_A (fF/nm) C_F (fF/nm) C_C (fF/nm)							
#							
cap	M2	SUB	200	200	6.3343E-06	4.7426E-06	1.2833E-04
cap	M2	SUB	200	400	6.0743E-06	7.3642E-06	6.2607E-05
cap	M2	SUB	200	600	6.1229E-06	9.6100E-06	4.4632E-05
cap	M2	SUB	200	800	6.0743E-06	1.1713E-05	3.5030E-05

Figure 4-2 – Example of a foundry table, *metal1* above *substrate* (M1/ SUB) for the UMC 130nm.

The problem with this data is the small range of values for the look-up variables, which only include four different values of width, and eight different values of space for each one of those widths. If the table is accessed with values for both width and space different from the available ones, the results have to be computed somehow.

To create a general model to for these tables that can access the intercalary values, the different Area (C_A), Fringe (C_F) and Coupling Capacitances (C_C) were graphically represented in Figure 4-3, Figure 4-4 and Figure 4-5, respectively, according to the values of width and space, using Matlab®. In the following graphs the different colors illustrate different widths.

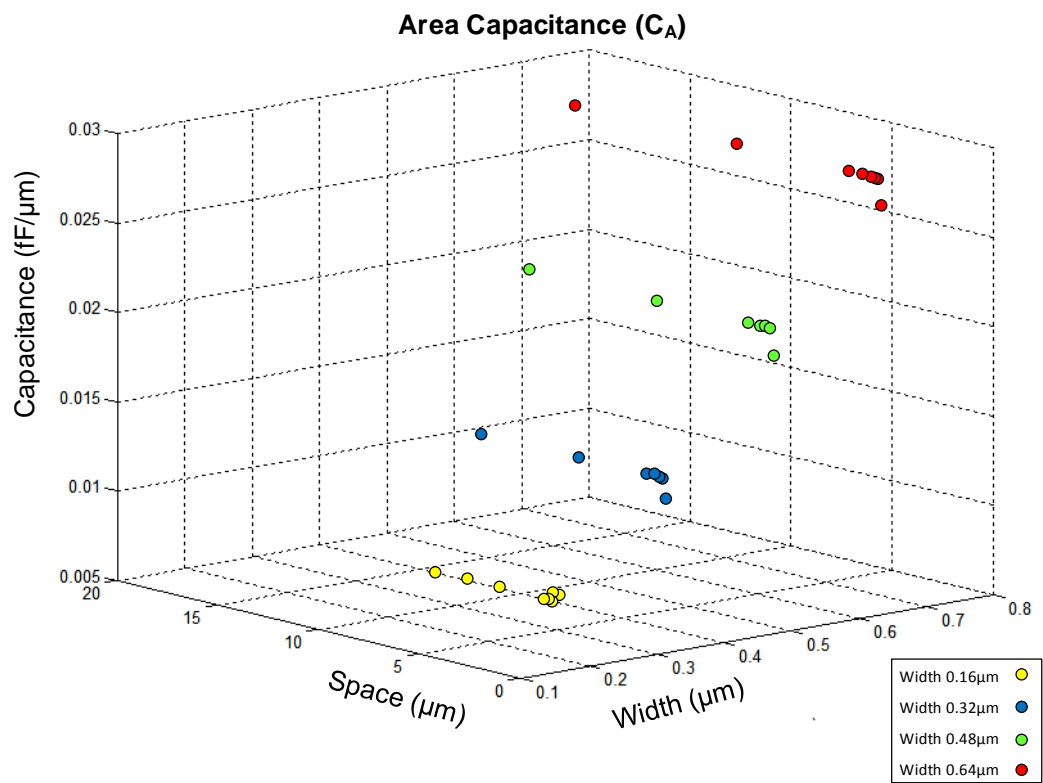


Figure 4-3 – 3-D representation of Area Capacitance.

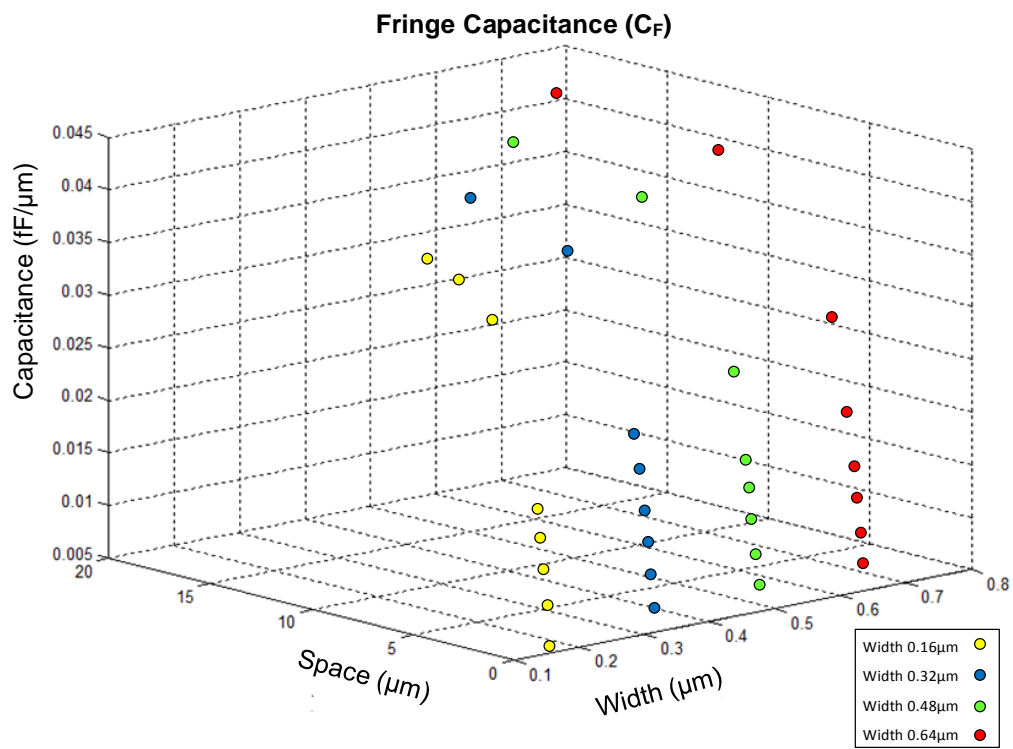


Figure 4-4 – 3-D representation of Fringe Capacitance.

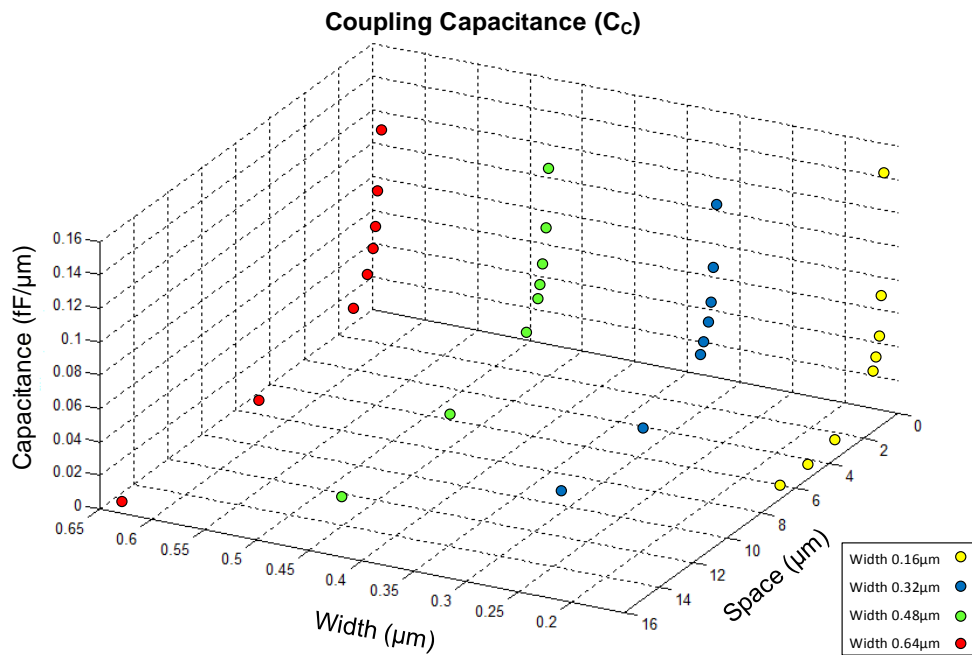


Figure 4-5 – 3-D representation of Coupling Capacitance.

Evaluating the 3D graphs, it can be concluded that maybe the values for the capacitance depend more on one variable than the other, being that variable width or space. If the values depend more on one variable maybe the other can be discarded so we end up with an easier interpolation. To validate this premise, the variable suspected to be less relevant was removed so that a 2-D representation of the same data was visible, starting by C_A .

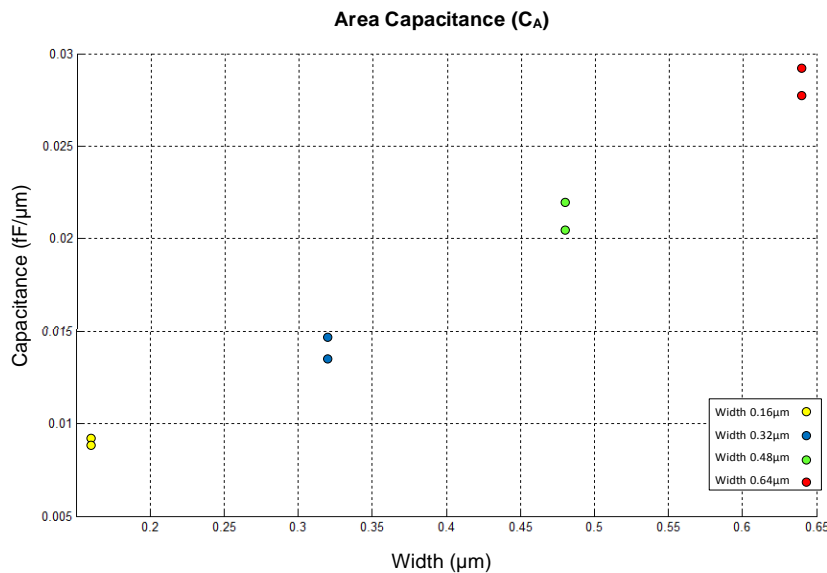


Figure 4-6 – 2-D representation of Area Capacitance.

It is easily observed in Figure 4-6 that the values are almost constant relative to the changing of the values of space, so it's acceptable to discard this variable. In the 2D graph above (Figure 4-7), the proximity of the points confirms there is no need to consider space, and interpolating linearly by segments over width, the results are the blue lines.

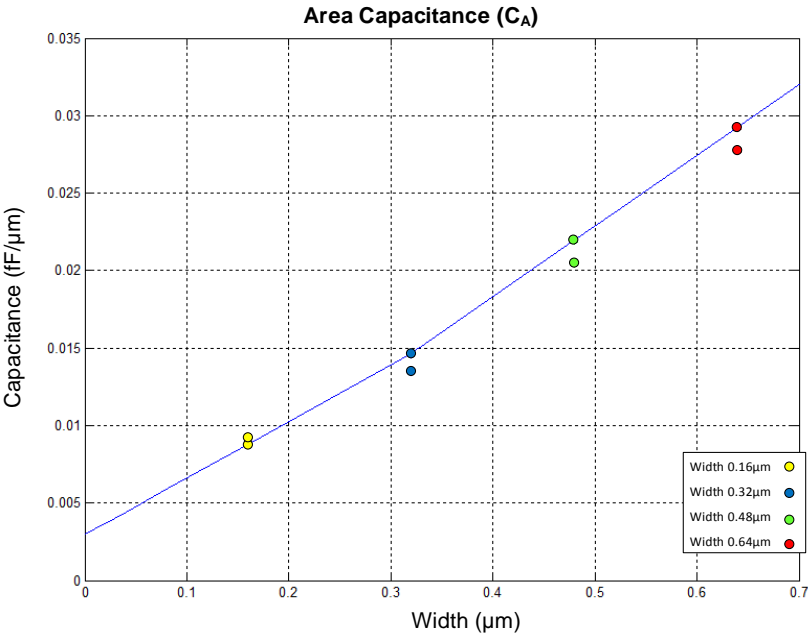


Figure 4-7 – Linear-by-segments interpolation of Area Capacitance.

Evaluating now the Fringe Capacitance in Figure 4-8, it can be concluded that maybe the width variable can be discarded without adding much error to the values.

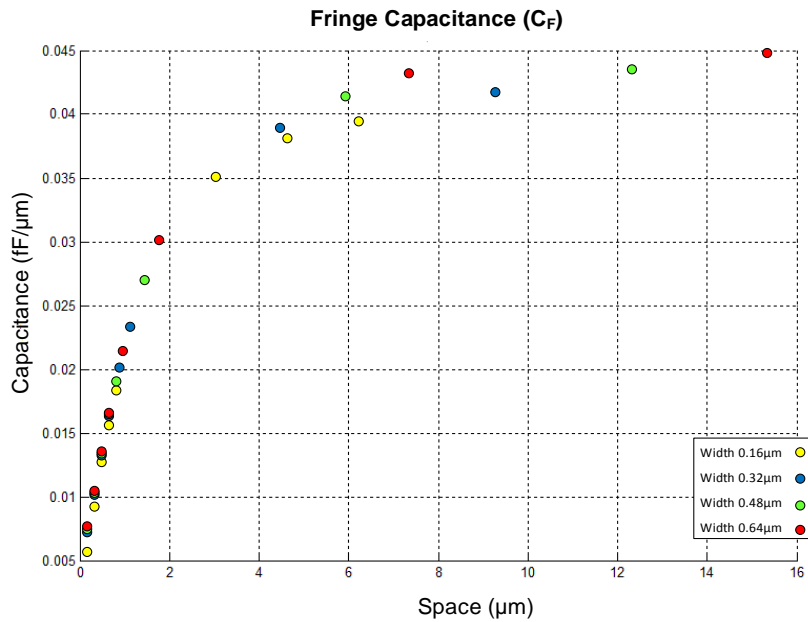


Figure 4-8 – 2-D representation of Fringe Capacitance.

The form of the aggregated points suggests that a nonlinear interpolation to a logarithmic function should work, but since there's a great concentration of points, a linear-by-segments interpolation approximates that function well enough so that complicated nonlinear interpolations are avoided. The results for this simpler approximation are shown in Figure 4-9.

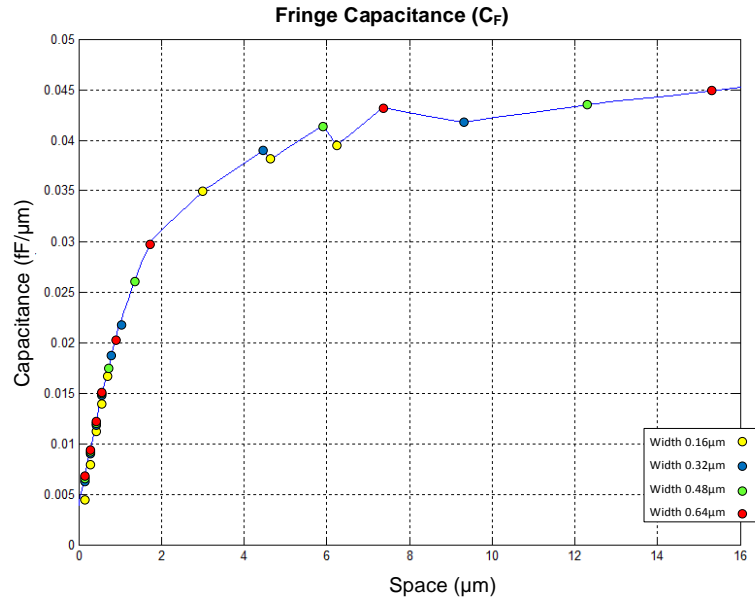


Figure 4-9 – Linear-by-segments interpolation of Fringe Capacitance.

As Fringe Capacitance, the Coupling Capacitance illustrated in Figure 4-10 shows that the dependence on the space variable is way greater than on the width variable, suggesting again that the removal of that variable simplifies the interpolation without adding relevant error to the estimation.

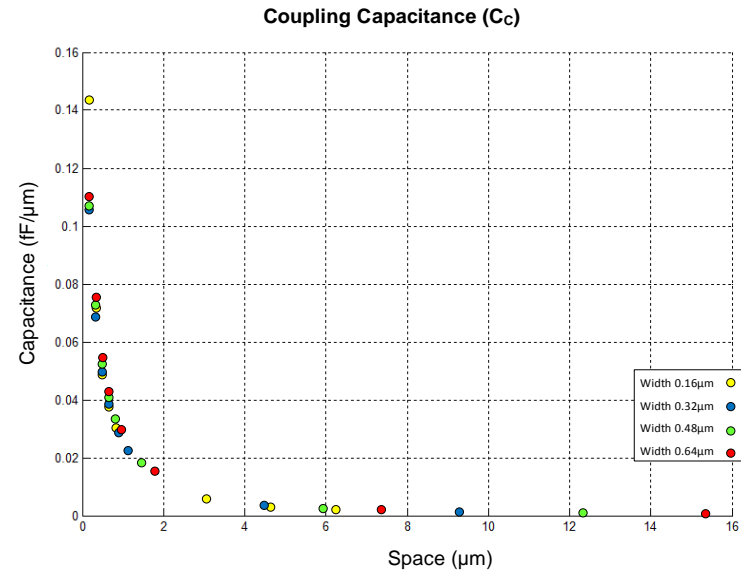


Figure 4-10 – 2-D representation of Coupling Capacitance.

This aggregation of points, as performed before for C_F , suggests a nonlinear approximation, in this case an exponential function, but the graph in Figure 4-11 shows that again a linear-by-segments interpolation approximates this function very well, due to the large quantity of experiment points.

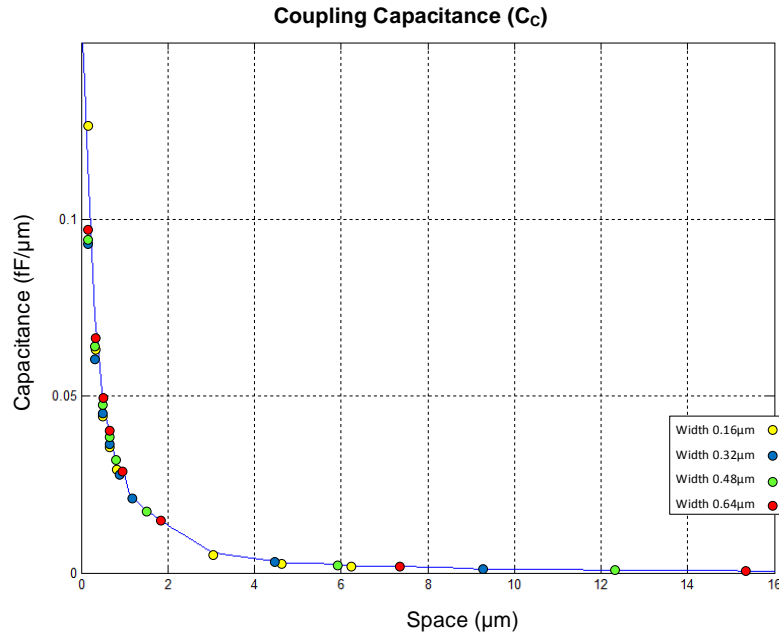


Figure 4-11 – Linear-by-segments interpolation of Coupling Capacitance.

4.2 Preliminary tests

Using a built-in extractor to be embedded in the optimization loop and guide the optimization, it is crucial to accurately estimate circuit's parasitics. Designers trust in industry “standard” extraction tools, especially on Mentor Graphics’ Calibre®, so the AIDA-PEX tool has to approximate as much as possible the values of this off-the-shelf extractor. The following case studies evaluate the capacitances extracted by Calibre® in various situations where two plates are strategically positioned.

4.2.1 Case Study I: Two parallel stripes of Metal (1, 4, 8)

In this experiment two parallel stripes of the same metal were drawn with the same size, according to the empirical data for *metal1*, with a $0.32\mu\text{m}$ width and spaced by $0.32\mu\text{m}$. The length was chosen for practical reasons and has a value for all stripes of $100\mu\text{m}$.

The main goal of this experiment was to compare the results for the intrinsic and interconnect capacitances extracted by Calibre® and the ones calculated by interpolation of the empirical data from the design kits of the technology. The extracted data from these tables to each measurement was the Area Capacitance (C_A), the Coupling Capacitance (C_C) and two Fringing

Capacitances (C_F), one considering the $0.32\mu\text{m}$ spacing to the other stripe, and the other considering the maximum spacing presented in the data for the empty side of the stripe. The intrinsic capacitance is calculated by adding C_A and both C_F 's, as illustrated in Figure 4-12.

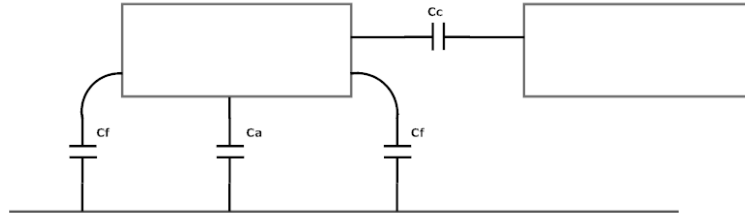


Figure 4-12 – Capacitances considered on Case Study I.

The results for this test are presented in Table 4-1. For the *metal1* test the values were directly retreated from the foundry tables, but for the other two the values of width and space were different from the ones available, so the values for the capacitances had to be interpolated. Even so, the errors show promising approximations for these situations.

Table 4-1 – Results for Case Study I.

Conductor Stripes	Calculated (Empirical method)		Experimental (Calibre (R))		Relative Error C_c (%)	Relative Error C_i (%)
	C_c (fF)	C_i (fF)	C_c (fF)	C_i (fF)		
Metal 1	6.885	6.661	7.282	5.382	-5.442	+23.746
Metal 4	6.972	3,777	8.834	3.001	-21.085	+25,877
Metal 8	25.52	1,912	23.187	2.389	-10.062	-19,936

A second goal was set and an extra parameter was added to the table: Lateral Overlap. Sliding the second stripe of *metal1* on a parallel way (as shown in Figure 4-13) and using this extra variable, we can compare the results with the calculations to see if there is a linear relationship.

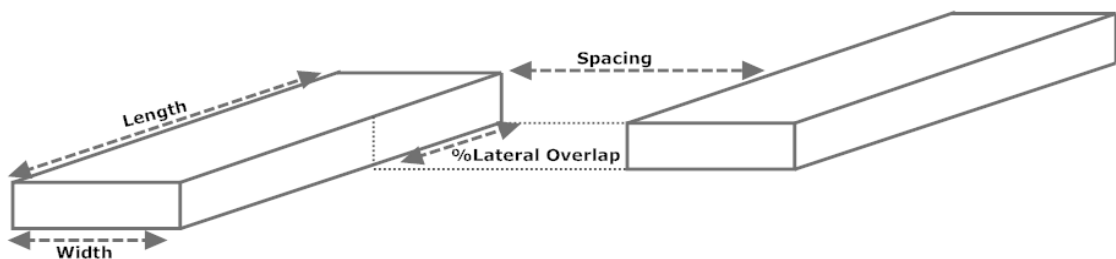


Figure 4-13 – Geometrical parameters on parallel slide.

Comparing the values of C_C for the “parallel sliding stripe” part of the experiment in Table 4-2, it can be concluded that there is a simple linear relation between Lateral Overlap and Lateral Capacitance (C_C in this case), because the error is always the same, so with 50% of Lateral Overlap, the Coupling Capacitance reaches 50% of the initial value.

Table 4-2 – Results for parallel slide.

Lateral Overlap (%)	Calculated (Empirical method)		Experimental (Calibre (R))		Relative Error C_C (%)	Relative Error C_i (%)
	C_C (fF)	C_i (fF)	C_C (fF)	C_i (fF)		
100	6.885	6.661	7.28	5.382	-5.442	+23.747
50	3.443	6.661	3.64	6.097	-5.442	+9.243
25	1.721	6.661	1.82	6.454	-5.442	+3.195
0	0	6.661	0	6.812	-5.442	-2.218

With the good results of the “parallel sliding stripe” experiment, it was natural to ask what would happen to the parasitic capacitance when the spacing between the stripes increases, so another experiment was conducted as it is shown in Figure 4-14.

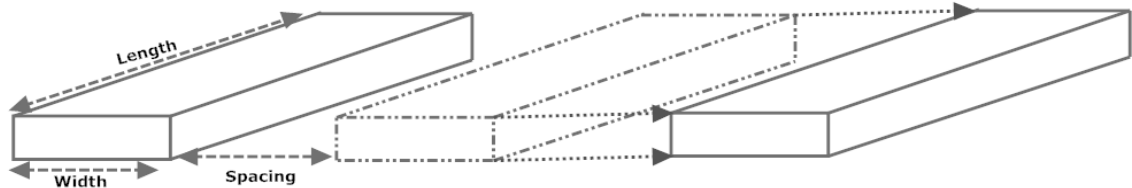


Figure 4-14 – Geometrical parameters on perpendicular slide.

The results for this experiment are presented in Table 4-3, where calculations with both linear interpolation and linear-by-segments interpolation were compared with the values extracted by Calibre®. It became clear there is a problem with the linear regression applied on the data extracted from the tabled C_C , which reaches errors of 350%. This problem occurred because the data had an exponential type function and was approximated by a linear model, whereas with the linear-by-segments interpolation, the exponential function is almost perfectly replicated.

With this first case study the chosen regression to approximate the design kit tables was tested and the relative errors support this estimation. It can be also concluded that in Calibre® whenever two stripes are separated by a distance greater than $3\mu\text{m}$ the coupling capacitance is always considered 0. In the next case studies, a direct comparison is impossible without further geometrical consideration, and the purpose was to understand how certain capacitances

change in certain situations.

Table 4-3 – Results for perpendicular slide.

Spacing (μm)	Calculated (Empirical, Linear regression)		Calculated (Empirical, Linear-by- segments interpolation)		Experimental (Calibre (R))		Linear regression		Linear-by- segments regression	
	Cc (fF)	Ci (fF)	Cc (fF)	Ci (fF)	Cc (fF)	Ci (fF)	Relative Error Cc (%)	Relative Error Ci (%)	Relative Error Cc (%)	Relative Error Ci (%)
0.32	6,885	6,661	6,885	6.661	7.281	5.382	-5,44	+23,75	-5,44	+23.75
0.64	4,297	7,275	3,843	7.274	4.002	5.989	+7,38	+21,46	-3,96	+21.46
0.96	3,928	7,788	2,956	7.458	2.542	6.454	+54,52	+20,67	+16,28	+15.55
1.28	3,559	8,16	2,027	7.657	1.703	6.784	+108,96	+20,29	+18,98	+12.87
1.6	3,190	8,5	1,68	7.856	1.186	6.998	+168,96	+21,47	+41,64	+12.27
1.92	2,821	8,716	1,415	8.056	0.854	7.121	+230,31	+22,39	+65,69	+13.13
2.24	2,452	8,84	1,172	8.255	0.634	7.176	+286,82	+23,19	+84,85	+15.04
2.56	2,083	8,965	0,929	8.456	0.484	7.181	+330,77	+24,84	+91,97	+17.73
2.88	1,714	9,089	0,685	8.654	0.378	7.152	+353,31	+27,09	+81,12	+21.01
3	1,576	9,136	0,594	8.728	0.349	7.134	+354,31	+28,05	+71,15	+22.35
3.1	1,461	9,168	0,569	8.791	0	6.812	(inf)	+34,59	(inf)	+29.06

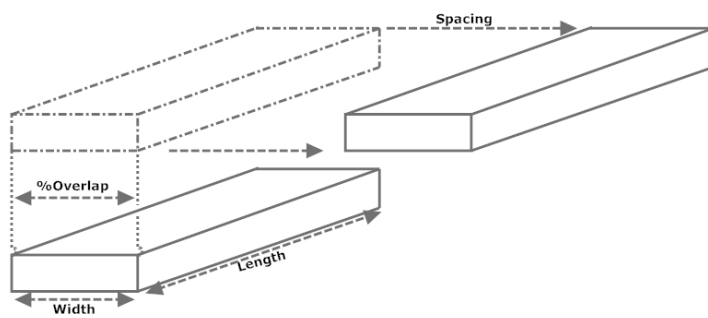
4.2.2 Case Study II: Stripe of Metal X above a Stripe of Metal 1 (parallel)

For this experiment two stripes of adjacent metals were drawn with the same size (width: $2\mu\text{m}$, length: $100\mu\text{m}$) and placed one above the other, where initially the one on top completely overlaps the one on the bottom. This test was then repeated replacing the top stripe for higher layers to compare the values, as it's presented on Table 4-4.

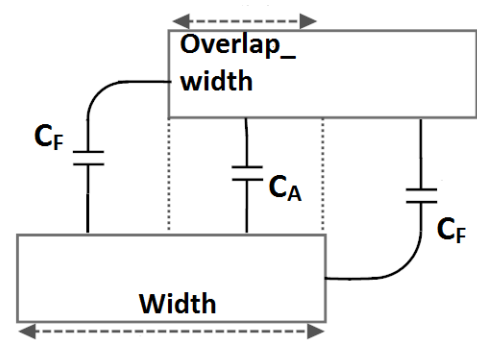
For the second part of this experiment the higher metal stripe (in this test only *metal2* was used) was moved perpendicularly, as illustrated in Figure 4-15, so the overlap is consecutively reduced until it reaches zero, and then spacing starts to increase as the plate continues to be moved. Doing that, the area component of the interconnect capacitance decreases as the fringe component increases. When the overlap width percentage reaches zero, the area component vanishes and only fringe capacitance is considered.

Table 4-4 – Results for Case Study II (Part I).

Higher Conductor Stripe	Width (um)	Length (um)	Calibre (R)		
			Ci M1 (fF)	Ci MX (fF)	Cc (fF)
Metal 2 over Metal1	2	100	13.294	5.266	24.063
Metal 3 over Metal1			14.719	4.724	8.785
Metal 4 over Metal1			15.582	4.343	5.451
Metal 5 over Metal1			16.171	4.051	3.958
Metal 6 over Metal1			16.599	3.822	3.019
Metal 7 over Metal1			15.408	0.074	4.446
Metal 8 over Metal1			17.516	3.601	1.754



(a) 3-D view. Geometrical parameters.



(b) 2-D view. Capacitances.

Figure 4-15 – Parameters took into account on Case Study II.

The results for this experiment are presented in Table 4-5, where it is clear that the intrinsic capacitance of the lower stripe slightly increases with the sliding of the upper one, since the fringe component that in the beginning composed the interconnect capacitance between the conductors, started to turn its effect to the substrate capacitance. For the substrate capacitance of the upper stripe, it is obvious the value increases faster because in the beginning there is a stripe right below, and iteratively the space below opens with the slide. For the interconnect capacitance, it became clear that the area component has a stronger effect than the fringe one, and that Calibre® uses different models due to the drastic gap between the values $0.018\mu\text{m}$ and $0.019\mu\text{m}$ of spacing.

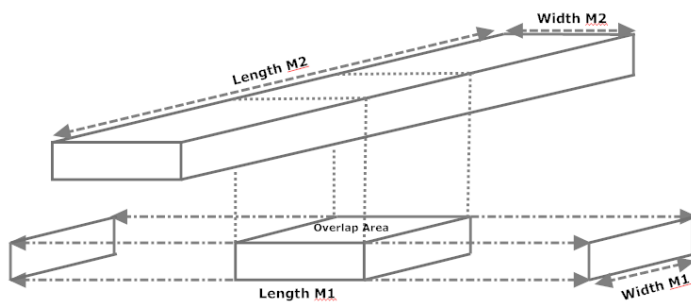
4.2.3 Case Study III: Stripe of Metal 2 above a Stripe of Metal 1 (perpendicular)

For this experiment a strip of *metal2* was drawn (width: $1\mu\text{m}$, length: $10\mu\text{m}$) and a squared stripe of *metal1* was added underneath and in the center so it's completely overlapped by the *metal2* one, and as it's presented in Figure 4-16. This stripe stops being a square and grows perpendicularly to the other one, so the width of the *metal1* stripe is fixed ($1\mu\text{m}$) and the length

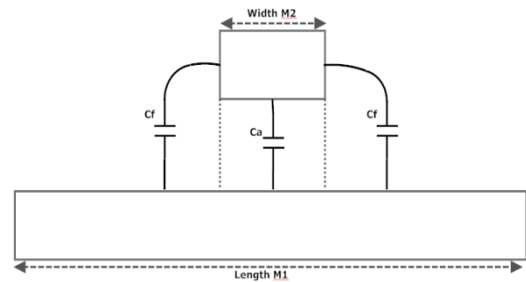
is the increasing variable.

Table 4-5 – Results for Case Study II (Part II).

Width (um)	Length (um)	Spacing (um)	Overlap (%)	Calibre (R)		
				Ci M1 (fF)	Ci M2 (fF)	Cc (fF)
2	100	0	100	13.294	5.266	24.063
		0	50	14.335	4.381	17.546
		0	25	14.346	5.594	12.606
		0	10	14.353	6.321	9.594
		0	5	14.355	6.564	8.586
		0	2.5	14.356	6.685	8.082
		0	0	14.357	6.806	7.577
		0.01	0	14.357	6.831	7.476
		0.018	0	14.357	6.849	7.385
		0.019	0	14.357	7.628	9.344
		0.05	0	14.793	8.078	9.077
		0.1	0	14.799	8.088	8.663
		0.2	0	14.825	8.128	7.901
		0.5	0	14.973	8.352	6.054
		1	0	15.268	8.806	4.029
		2	0	15.768	9.606	2.079



(a) 3-D view. Geometrical parameters.



(b) 2-D view. Capacitances.

Figure 4-16 – Parameters took into account on Case Study III.

The results for this experiment are presented in Table 4-6, where it was concluded that the substrate capacitance is directly proportional to the length of the stripe. Moreover, the fringe capacitance has a small effect in the interconnect capacitance and for spacing larger than $3\mu\text{m}$ the effect ceases to exist, and the interconnect remains constant.

Table 4-6 – Results for *Case Study III*.

Width M1 (μm)	Length M1 (μm)	Width M2 (μm)	Length M2 (μm)	Overlap (%)	Calibre (R)		
					Ci M1 (fF)	Ci M2 (fF)	Cc (fF)
1	1	1	10	100	0.126	0.751	0.215
	2			50	0.25	0.701	0.248
	3			33	0.356	0.701	0.252
	4			25	0.459	0.701	0.253
	5			20	0.563	0.701	0.253
	8			12.5	0.874	0.701	0.253
	10			10	1.082	0.701	0.253
	20			5	2.119	0.701	0.253

4.3 Conclusions

The extractor uses an empirical-based method based on look-up tables processed from the design kit of the technology, so those tables were introduced and the new interpolation of the data was illustrated. Unlike previous works, the proposed approach allows the interpolation to be simple but with a good accuracy for the data retreated from the tables. From the capacitances extracted, it is concluded that the fringe components are the hardest to compute and replicate.

This experiments served as an introduction to the capacitance modeling and to understand how the different components of interconnect and intrinsic capacitance change in the various situations. Moreover, the empirical method chosen was tested and supported by the results, where with other geometrical considerations the values can improve to achieve the desired accuracy.

Chapter 5 Parasitic Extraction

In this chapter, the detailed models for parasitic resistance and capacitance are outlined. Then, the geometrical concerns are presented.

The inclusion of layout-related data is crucial to achieve a first-time-right design at the end of the optimization loop, trimming down the impact of parasitic devices in analog circuits' performance and providing accurate geometrical layout properties, e.g. area, aspect ratio, etc.

Using an embedded extractor, it is of the utmost importance to derive reliable estimates for the parasitics that can compete with the accuracy of standard industry tools. As presented in Figure 5-1, the main tasks of the parasitic extraction are resistance and capacitance estimation, along with the geometrical considerations needed to accurately extract the circuit's parasitics.

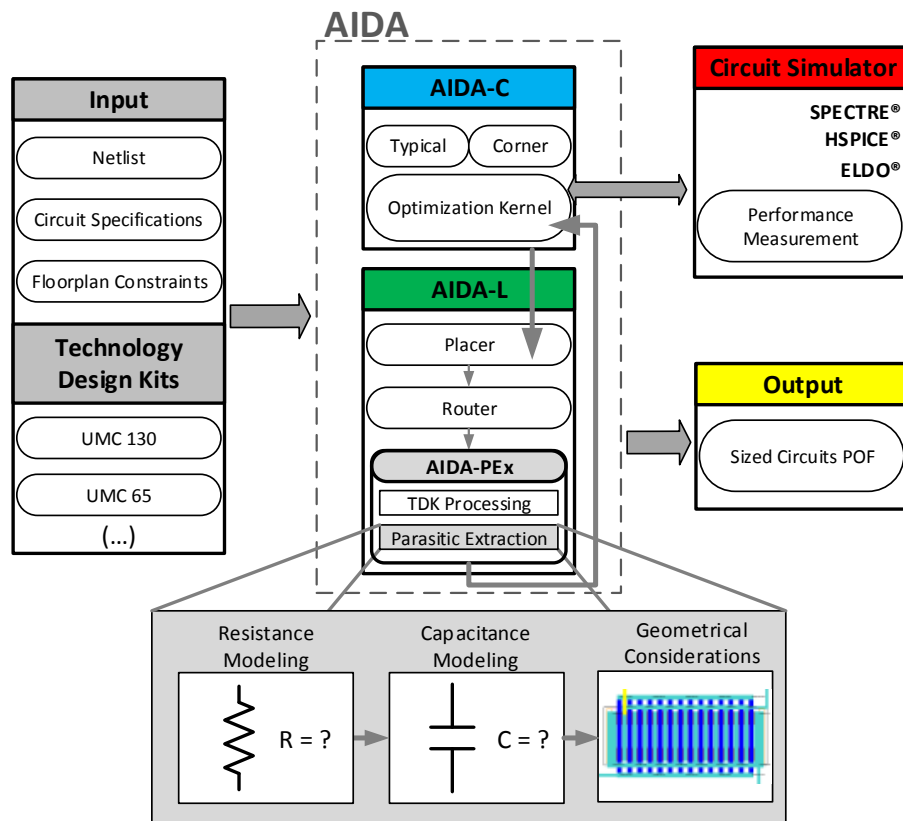


Figure 5-1 –Parasitic extractor architecture: Resistance Modeling, Capacitance Modeling, Geometrical Considerations.

Although this is not a sequential flow and these three sub-blocks are processed simultaneously, in the next subsections the resistance estimation (Section 5.1), capacitance estimation (Section 5.2) and geometrical considerations (Section 5.3) are detailed. From the work developed before [3], the resistances estimated showed consistent approximation and the greater discrepancies

relied on capacitance estimation for higher complexity layout modules (e.g. interdigitation or common centroid).

5.1 Parasitic Resistance

In analog design of ICs, the components of a circuit are all conductor stripes, and conductors have intrinsic resistance dependent of its characteristics, as illustrated in Figure 5-2. Parasitic resistance is an undesirable and unintended consequence of putting a design integrated circuit concept into manufacturing.

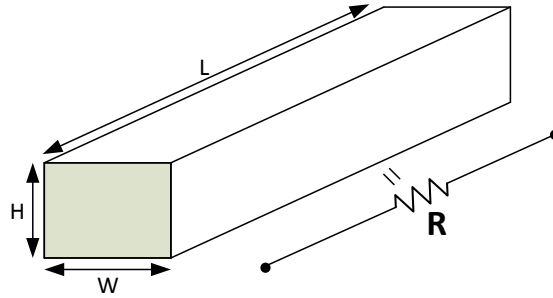


Figure 5-2 – Intrinsic resistance of a conductor.

The resistance in a conductor is a function of the conductor's cross section area, its resistivity/conductivity (dependent on the stripe's material) and length:

$$R = \rho \frac{L}{W \times H} \quad (1)$$

This resistance is also directly proportional to the temperature of the conductor, and this factor is already included in the resistivity constant ρ . This is a well defined formula and the results are easy to compute if the geometrical parameters used, for bigger components containing large number of conductors, don't become a tiresome task to extract from a layout.

To correctly estimate the circuit's parasitic resistance, layout components were separated into two sections: the device's terminals and the routing wires. For the device terminal shapes the RF transistor module was imported:

$$R_{drain} = R_{source} = 150.35 \times 10^{-6} \times w_g \times nf \quad (2)$$

where w_g is the width of the gate and nf is the number of fingers for that transistor. With these equations the intra-module resistance is dealt with. For the routing the estimation is not so trivial. The parasitic resistance for each wire segment R_{wire} , which is defined by a width and length, is computed directly from the resistance per unit square R_c tabulated for a given

conductor, at a temperature T :

$$R_{wire} = R_c(T) \times \frac{length}{width} \quad (3)$$

Each wire has any number of segments/bends, so all partial resistance components are considered for square counting, as illustrated on Figure 5-3.

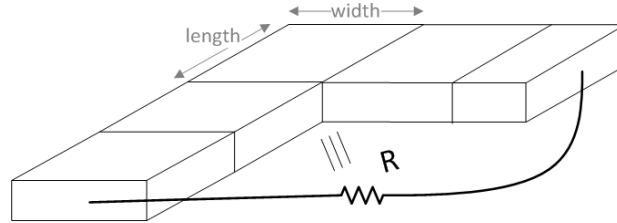


Figure 5-3 –Parasitic wire resistance computed by square counting [3].

The parasitic resistance estimation is quite straightforward and the real challenge lies on accurately extracting the parasitic capacitance of conductors.

5.2 Parasitic Capacitance

For MOS transistors it is common the use of geometric methods, where the device's width, length and number of fingers are used in an equation that provides the estimated parasitic. However, the technology-dependency of those equations, the difficulty found to derive them for more complex layout styles (e.g., common centroid) and the inapplicability to wires, forced a different approach. The chosen approach is an empirical-based technique, where several realistic 3-D effects (e.g., coupling capacitances between two interconnects, crossings in different conductors, etc.) are modeled as a combination of 2-D structures, for a 2.5-D modeling of the problem.

A conductor (or terminal) has an intrinsic capacitance relative to the substrate and an interconnect capacitance concerning each one of the nearby conductors. To calculate the values for these capacitances, all the conductors have to be evaluated two by two. Depending on the relative positioning of the conductors at issue, many situations can arise, leading to different classifications to the existing capacitances. To calculate interconnect and substrate capacitances, tree types of values can be extracted from the technology data: area capacitance (C_A), fringe capacitance (C_F) and coupling capacitance (C_C).

5.2.1 Substrate Capacitance (C_S)

Each conductor has an intrinsic capacitance considered to the plane below, being it the substrate, well or active area. When we want to calculate the intrinsic/substrate capacitance,

two types of capacitors can be differentiated: Area Capacitance (C_A), which covers the capacitances on the overlap area, right below the conductor, and Fringe Capacitance (C_F) which features all the other lines, as presented in Figure 5-4.

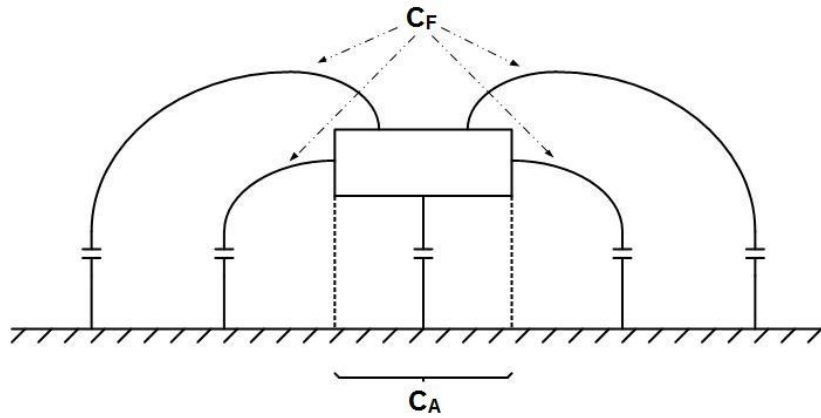


Figure 5-4 – Capacitances considered to compute substrate capacitance.

As referred, these capacitors and their characteristics relate to the electric field lines, so it becomes obvious that the value of the capacitance will be greater where the density of field lines is bigger, so in this case it's expected that C_A will have a greater capacitance value than C_F . This capacitance is computed by the sum of the area and the two fringe components (4).

$$C_S = (C_A(\text{width}) \times \text{length}) + (2 \times C_F(\text{space}) \times \text{length}) \quad (4)$$

where the area capacitive component C_A is obtained by interpolation of the technology-dependent data provided in the foundry's TDks as a function of the conductor's width, and then computed over its length. The fringe component C_F is obtained by interpolation but with the space between the conductor and the closest shape in that same layer as a look-up variable.

5.2.2 Interconnect Capacitance (C_I)

It is defined as interconnect the capacitance between two conductors on different layers or in the same layer. To ensure that all shapes are evaluated and all capacitances covered, the tool performs three assessments: interconnect amongst terminals, amongst wires and interconnect between wires and terminals. The routing paths are chopped down into rectangular shapes and the terminals are sort out into the various *poly* and *metal1* shapes that define them. The conductors are then evaluated two by two and the partial capacitances are summed up in the end for each interconnect.

When the two conductors in question are in the same layer, as sketched in Figure 5-5, the Fringe components refer to the lines that exist from top-to-top and from bottom-to-bottom of the conductor stripes.

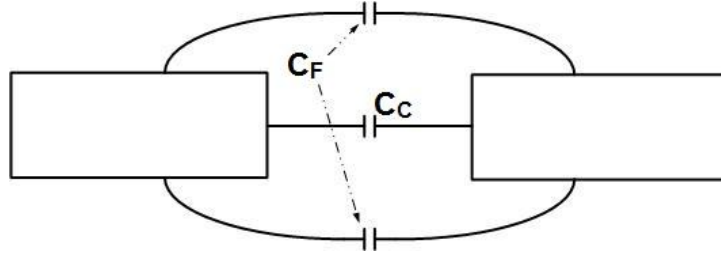


Figure 5-5 – Capacitances considered for interconnect capacitance on the same layer.

For the lines that go from side to side between the conductors, the capacitor is classified as Coupling Capacitance (C_C). Coupling capacitance is only present in this situation, because it refers to lateral overlap of the stripes. In this situation the fringe components are scorned and only C_C is considered:

$$C_I = (C_C(c_space) \times parallel_length) \quad (5)$$

where $C_C(c_space)$ is the coupling capacitive component obtained by the interpolation in conductor's c_space (space between conductors) of the foundry provided values, and $parallel_length$ is the length on which the two conductors laterally overlap.

If the conductors are in different layers the interconnect value depends on the area and fringe components between the two conductors, as indicated in (6). In this case, two situations can occur: Or the plates don't vertically overlap and only fringe components (C_F) are evaluated to come up with the interconnect capacitance; or they overlap and an area component (C_A) appears. As before, the area capacitance refers to the area between the plates and its value increases as the total overlap area increases. If the plates totally overlap, the value of the area capacitance is maximum and only side-to-side components of the fringe capacitance are present, which in most cases can be scorned.

$$C_I = (C_A(overlap_width) \times parallel_length) + (2 \times C_F(space) \times parallel_length) \quad (6)$$

For these distinct situations, different variables are considered. If the conductors overlap, $overlap_width$ is used as a look-up variable for C_A component, as shown in Figure 5-6. The fringe components C_F are interpolated again with the space between the higher plate and the closest shape in the same layer.

If the plates do not overlap the area component C_A vanishes and only C_F is considered to make the computation, as illustrated in Figure 5-7. In this case the equation used is the same (6) but only with the fringe part, and a new geometrical factor is deemed: c_space .

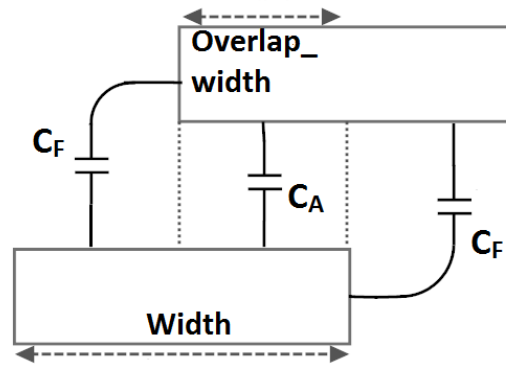


Figure 5-6 – Interconnect capacitance for overlapping plates (2D view).

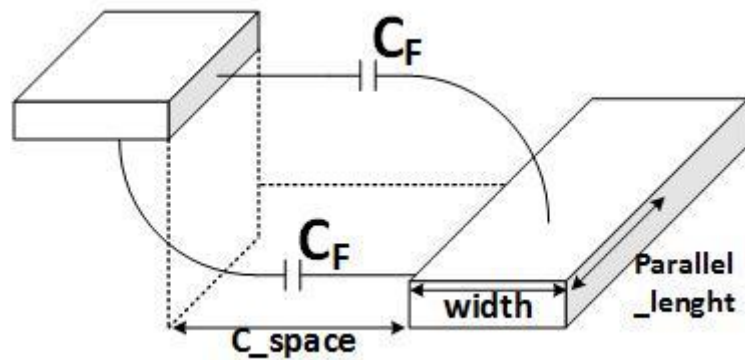


Figure 5-7 – Interconnect capacitance for non-overlapping plates (3D view).

The decay of C_F is approximately linear with the increase of space between conductors although the rate of decay is different for each pair of materials, as presented in Figure 5-8.

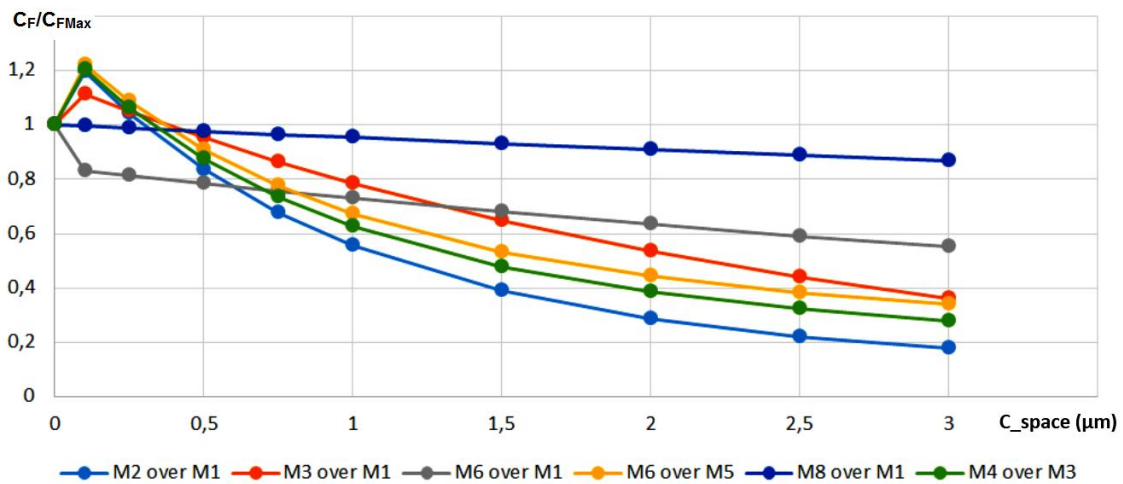


Figure 5-8 – C_F decay with respect to the space between conductors.

To address this decay a new factor has been added to the equation which is multiplied to the provided value from the foundry. Although the value of C_F doesn't depend much on the higher plate's width as concluded before, it does decay with the lower plate's width decrease. To see just how much the value of width influences the variation in C_F , a plate was placed at different c_space values (0, 0.5, 1, 1.5,...) initially with an infinite value of width (plates separated by more than $3\mu m$ are considered having no influence on each other, so if the lower plate has a width of $3.5\mu m$ or an infinite width the results are the same), and then reduced iteratively to observe the change. The results are illustrated on Figure 5-9.

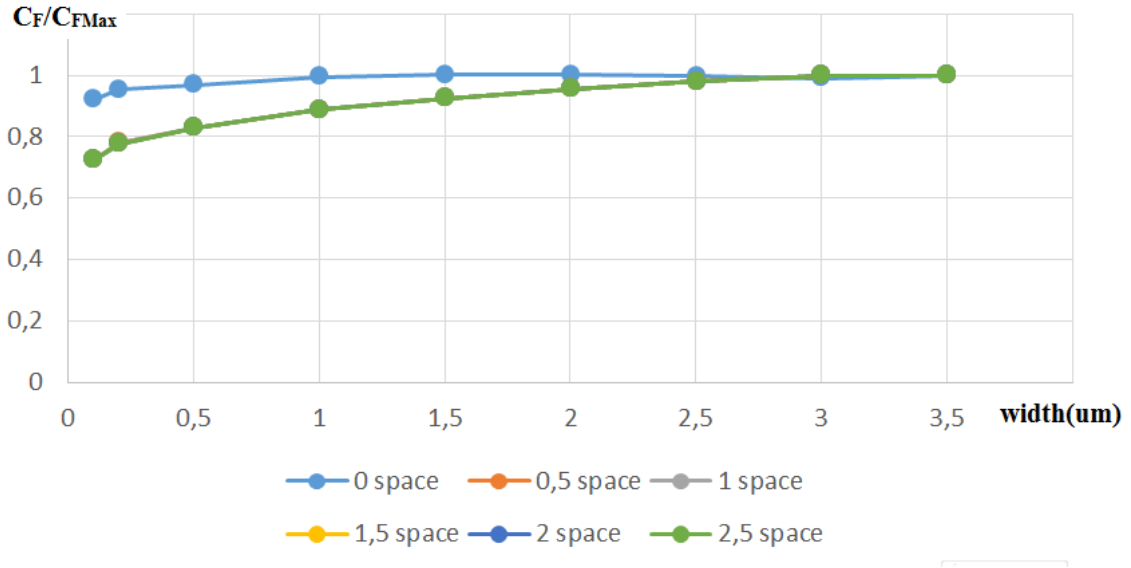


Figure 5-9 – C_F decay with respect to the lower plate's width.

In this picture is clear that the decay is roughly the same for every value of space but 0. With this in mind, a new decay factor that depends on the lower plate's width has to be added with a slope coefficient that is going to have only two possible values. The final equation to compute the interconnect capacitance related to fringe components is presented next:

$$C_l = 2 \times (C_F(space) \times (1 - \delta \times c_{space}) \times (w_0 + w_1 \times width)) \times parallel_length \quad (7)$$

where the green part corresponds to the decay due to the space between the conductors and δ is fitted depending on the type of shapes in evaluation. The red part corresponds to width related decay and w_0 and w_1 are fitted depending on which the space between the shapes is zero or not. This formulation is not only applied to this particular situation but to every situation where C_F is considered, depending on the geometrical factors. Revisiting equation (4), if the plate is not above active area or a well, it is considered that the substrate plate below is infinite to every direction, so C_F suffers no decay. Reviewing now equation (6), in that situation the

plate is either completely or partly below the other one so the plate is spitted in area and fringe part. The fringe part is always at $c_space = 0$ so the decay is well defined and this equation can be reformulated as in equation (8).

$$C_I = (C_A(overlap_{width}) \times parallel_{length}) + (2 \times C_F(space)(w_0 + w_1 \times width) \times parallel_{length}) \quad (8)$$

where w_0 and w_1 are fitted to the decrease of 0 space presented in Figure 5-9.

5.3 Geometrical considerations

To ensure the embedded tool approximates the values extracted by Mentor Graphics' Calibre®, a few more geometrical factors have to be taken into account. When two conductors are evaluated, not only their geometrical characteristics are being considered, but also the physical layout that surrounds them is being analyzed. For example to retreat the desired C_F value from the design kit tables the space between the conductor and the closest shape in that layer is used as a look-up variable, as said before. Another crucial consideration is space occupation in between the two conductors at issue, which is evaluated along the *parallel_length* area, as illustrated in Figure 5-10.

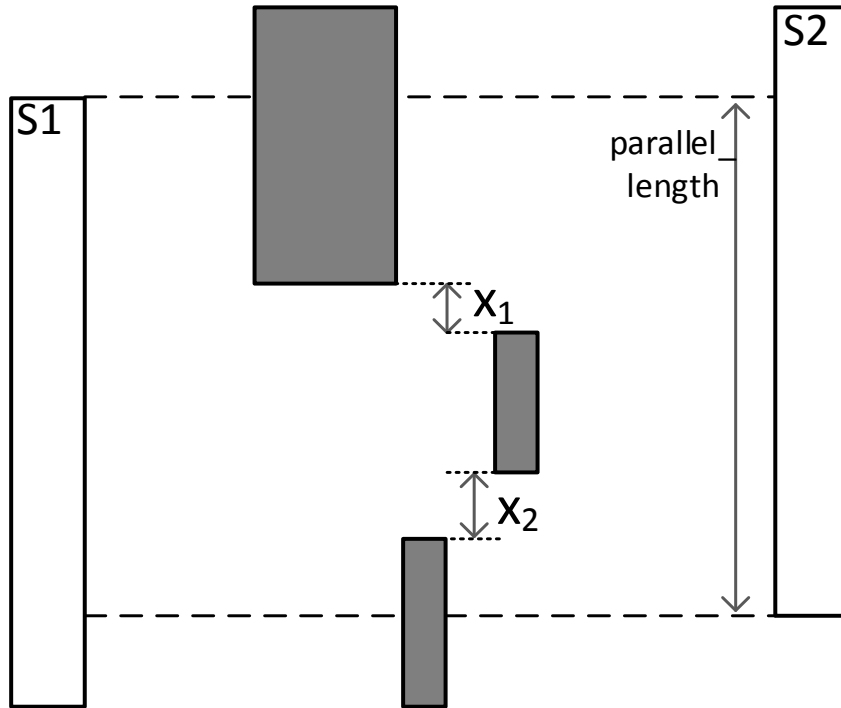


Figure 5-10 – Top view example of space occupation analysis.

In this example the interconnect capacitance is oriented in a horizontal way from one plate to the other, so the space occupation analysis is performed vertically. This geometrical module evaluates the vertical opened space and generates a percentage (9) that is later multiplied by the estimated interconnect capacitance.

$$P(\%) = \frac{\sum X}{parallel_length} \times 100 \quad (9)$$

Actually this evaluation is made even before the capacitance estimation, so not only the values for the interconnect capacitance are better fitted to the geometrical disposition, but also when the *parallel_length* area is totally obstructed the percentage is immediately zero and the parasitic estimation is not even executed.

AIDA-PEx has to work over a detailed routing as well as over the global routing created when the extraction is taking place inside the optimization loop. This global routing, as said before, doesn't account for wire overlap or design rule break, so additional geometrical concerns have to be made so that the extraction doesn't crash.

When two routing paths overlap (the routing paths of the global router are all done in *metal1* stripes), the best solution is to consider that in the final detailed layout one of them will be sketched in *metal2*, so a random path of the two is chosen and upgraded to the layer above for capacitance extraction purposes.

This is the solution for when the conductors overlap, but it can also happen that they don't overlap but run alongside each other at a distance smaller than the minimum permitted (or even at zero distance which would join the nets together). In this case it is considered that the paths are separated by the minimum distance allowed by the design rules.

5.4 Preliminary Tests

In this subsection, the intra-module capacitances (substrate and interconnect) are extracted in AIDA-PEx and in Calibre® for a set of NMOS and PMOS transistors with different specifications, to test the precision of the parasitic extraction inside the models, as presented in Table 5-1. It was decided to conduct this preliminary study for the capacitances of the transistors' terminals due the influence they have in the final net capacitances, which is bigger than the routing wire ones.

The error associated with interconnect capacitances doesn't exceed 11% but the intrinsic one reaches values of 39% of the intended value. Yet, the bigger values of relative error occur for very small values of capacitances, values that are smaller than 1 fento Farad, so this error won't have a great influence on the performance of the circuit.

Table 5-1 – Intra-module Capacitance Comparison.

Module	Terminal	AIDA Pex (fF)			Calibre Pex (fF)			Relative Error (%)	
		C _s ¹	Coup. Net	C _i ²	C _s	Coup. Net	C _i	C _s	C _i
N-MOS l=30u w=0,2u nf=8	Source	0,243	Gate	1,372	0,192	Gate	1,425	+26,563	-3,719
	Gate	1,589	Drain	1,331	1,76	Drain	1,363	-9,716	-2,348
	Drain	0,099	Source	2,481	0,086	Source	2,397	+15,116	+3,504
P-MOS l=50u w=0,2u nf=4	Source	0,756	Gate	1,594	0,865	Gate	1,778	-12,601	-10,349
	Gate	0,711	Drain	1,555	0,749	Drain	1,688	-5,073	-7,879
	Drain	0,05	Source	3,854	0,037	Source	3,651	+35,135	+5,56
P-MOS l=100u w=0,2u nf=30	Source	0,502	Gate	4,915	0,653	Gate	4,984	-23,124	-1,384
	Gate	5,196	Drain	4,877	6,553	Drain	4,913	-20,708	-0,733
	Drain	0,37	Source	8,451	0,338	Source	8,323	+9,467	+1,538

¹ – Substrate capacitance ² – Interconnect capacitance

5.5 Conclusions

In this chapter, the methodology used by the proposed parasitic extractor was described, along with the steps that led to the respective modeling. The equations considered in the model for the estimated parasitic resistances and capacitances, along with the geometrical factors were presented.

Avoiding the need for the detailed routing in the optimization process, the best quality of AIDA-PEx is the possibility to work over a global routed layout, which largely accelerates the process due to the difference of time that takes to get a simplistic global routing instead of a complete detailed one.

Chapter 6 Results

In this chapter the experimental results of the proposed parasitic extractor for some example circuits are presented.

The framework of the proposed methodology for the parasitic extractor of analog ICs layout, based on foundry data and empirical models, has been coded in JAVA™. In both examples, the experimental results are compared with Mentor Graphics Calibre® to validate the accuracy of the approach. Also, when comparing results obtained with AIDA-PEX and Calibre®, it is important to keep in mind that AIDA-PEX extractions were done over layouts with only global routing, and, the ones in Calibre® were done over complete layouts with the detailed routing in place.

6.1 Case Study I – Single Ended 2-Stage Amplifier

The first circuit used as test case is a single ended 2-stage amplifier. The amplifier schematic is presented in Figure 6-1 (a) and was designed for UMC 130 nm CMOS technology. This circuit was optimized for maximum gain and minimum area with AIDA layout-aware, resulting in the Pareto optimal front (POF) of sizing solutions illustrated in Figure 6-1 (b).

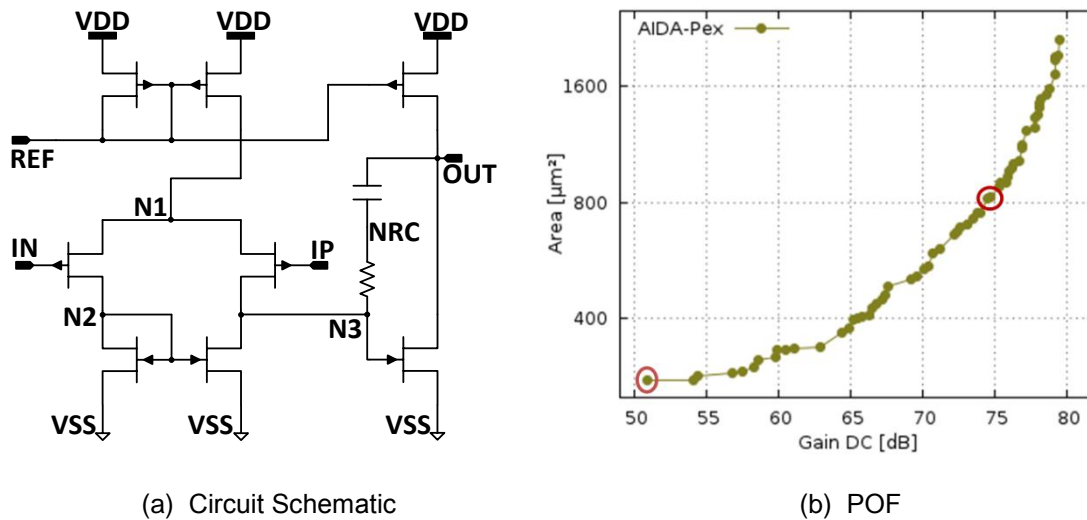


Figure 6-1 – Single ended 2-stage amplifier used as respective POF.

From this POF two points were chosen with different layout dispositions, one of them with the smallest area available and 51dB of gain and the other in the middle of the POF data line with 75dB of gain (Figure 6-1 (b)), to compare the estimated capacitances with the ones extracted by Calibre®.

In Table 6-1 the results for the direct comparison between AIDA-PEX and Calibre® for the bulk capacitance of both layout implementations are presented.

In this table it is clear that the error is higher in the second sizing, where the components have bigger dimensions and consequently the routings have a higher contrast, so the circuit is more susceptible to parasitic effects. For the interconnect capacitances between nets for the first implementation, the results are presented on Table 6-2.

Table 6-1 – Direct Bulk Capacitance Comparison.

Layout	Net	REF	D11	IP	IN	D12	D12R	NETZ53	OUT
51dB	AIDA-PEX (fF)	6,945	1,873	0,455	0,436	1,2	1,477	0,638	1,716
	Calibre (fF)	7,115	1,713	0,389	0,389	0,903	1,129	0,581	1,884
	Absolut Error (fF)	-0,17	+0,159	+0,065	+0,047	+0,297	0,3477	+0,056	-0,168
	Relative Error (%)	-2,39	+9,308	+16,79	+11,94	+32,93	+30,79	+9,624	-8,903
75dB	AIDA-PEX (fF)	15,956	5,262	3,391	3,394	2,444	1,906	2,145	3,103
	Calibre (fF)	19,864	8,709	3,61	3,61	4,703	1,561	6,841	2,814
	Absolut Error (fF)	-3,908	-3,447	-0,219	-0,216	-2,259	+0,345	-4,696	+0,289
	Relative Error (%)	-19,67	-39,58	-6,066	-5,983	-48,03	+22,1	-68,64	+10,27

Table 6-2 – Direct Interconnect Capacitance Comparison for 51dB Layout.

		Calibre®									
AIDA-PEX	NET	REF	N2	IP	IN	N3	NRC	N1	VDD	VSS	OUT
	REF		0	0,03	0	0,238	0	0,355	3,414	0	2,372
	N2	0,009		0,0407	0,2799	0,252	0	0,465	0,114	0,899	0
	IP	0,026	0,097		0	0,222	0	0,261	0,052	0,001	0
	IN	0	0,278	0,009		0	0	0,297	0,026	0	0
	N3	0,172	0,266	0,2	0		0,011	0,486	0,229	0,722	0,268
	NRC	0,002	0	0	0	0,018		0	0	0,002	0,021
	N1	0,359	0,449	0,224	0,224	0,384	0		1,216	0	0
	VDD	3,603	0,001	0,005	0	0,018	0,07	0,46		0,006	3,143
	VSS	0,003	0,802	0,031	0,136	0,503	0	0,01	0,002		0,424
	OUT	3,044	0	0	0	0,412	0,036	0,015	3,397	0,421	

In this table the interconnect capacitances net-to-net are directly compared, and the larger errors occur on the capacitances to the power nets. In Table 6-3 the same results are presented

to the 75dB sizing. Considering that the layouts used for the two extractors have slightly different routing paths, the results are promising. Although there are still some cases where the capacitances diverge, the extracted values show sufficient approximation for the global router.

Table 6-3 – Direct Interconnect Capacitance Comparison for 75dB Layout.

	NET	Calibre®									
		REF	N2	IP	IN	N3	NRC	N1	VDD	VSS	OUT
AIDA-PEx	REF		0,195	0	0	0,054	0,046	0,917	9,596	0,002	7,196
	N2	0,464		0,155	2,255	1,363	0,006	0,892	1,159	1,928	0,003
	IP	0,003	0,152		0	2,249	0	2,196	0,176	0,017	0
	IN	0	2,547	0,029		0	0	2,209	0,191	0,018	0
	N3	0,091	1,305	2,511	0		0,175	0,747	0,916	0,805	0,729
	NRC	0,001	0,008	0	0	0,085		0	0	0	0,001
	N1	0,905	2,098	2,585	2,562	1,64	0		2,159	0,011	0
	VDD	9,407	0,011	0	0	0,004	0,049	0,384		0,594	0,908
	VSS	0,022	1,38	0	0,028	0,775	0,013	0	0		0,911
	OUT	7,938	0,003	0	0	0,819	0,288	0,008	2,143	1,045	

As stated, this circuit was optimized for maximum gain and minimum area using AIDA, where the resultant POF was illustrated in Figure 6-1(b). The results for the performance measurements for these two implementations are presented in Table 6-4, where the netlist resultant from the traditional simulation-based sizing is compared with the extracted netlists from AIDA-PEx and Calibre®, resultant from the layout-aware optimization-based sizing.

Table 6-4 – Pre/Post-Layout Simulation.

Specs		51 dB				75dB			
		Traditional		Layout-aware		Traditional		Layout-aware	
		Netlist	Calibre®	AIDA-PEx	Calibre®	Netlist	Calibre®	AIDA-PEx	Calibre®
Gdc	max ≥ 50 dB	53,7	53,7	50,9	50,9	75,4	75,4	74,6	74,6
Gbw	≥ 200 MHz	208,69	183,37*	204,29	206,30	206,68	182,66	209,25	210,05
Pm	≥55 °	55,56	46,42	74,27	73,54	57,83	58,27	64,51	60,56
Idd	≤ 200 μA	135,4	135,1	176,8	176,5	190,5	189,2	190,9	190,2
PSRR	≥ 55 dB	77,23	75,53	75,44	75,45	88,09	77,02	83,89	80,12
Voff	≤ 5 mV	3,8	3,83	4,39	4,39	4,83	4,91	5,02	4,38
No	≤ 600 μVrms	435,6	441,8	301,2	305,9	347,7	336,3	381,9	390,3
Sn	≤ 100 nV/√Hz	21,41	21,59	16,17	16,32	25,2	25,7	26,4	26,4

*Broken constraints

As it is clear in these tests, a small difference in certain capacitances (mostly referent to critical nets of the circuit) represents a great discrepancy in the performance evaluation of the circuit. The resulted POFs for the traditional simulation-based sizing and for the layout-aware synthesis are presented in Figure 6-2, and in Table 6-5 and Table 6-6 the resultant layouts for are portrayed, where the images are scaled for comparison purposes.

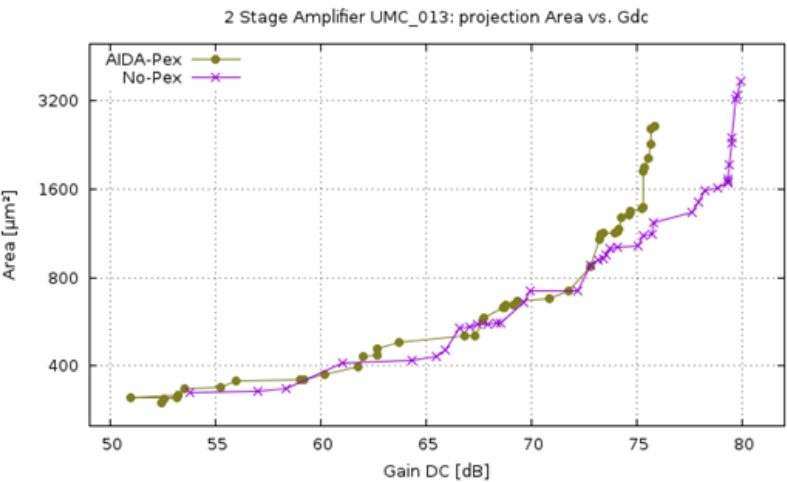
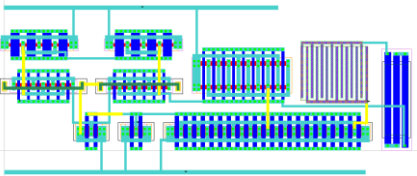
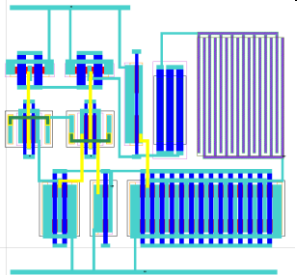


Figure 6-2 – Traditional and Layout-aware optimization POFs (Case Study I).

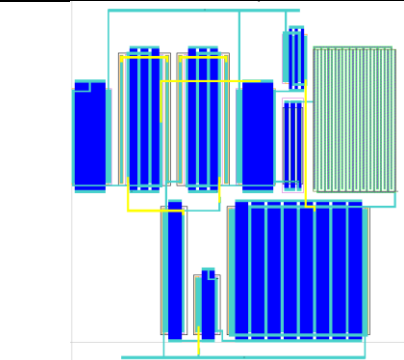
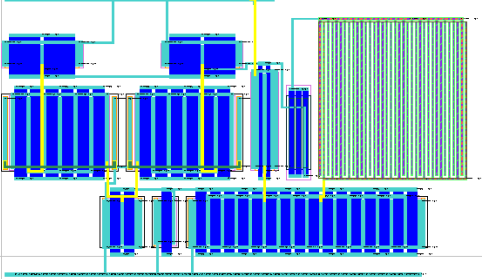
Table 6-5 – Illustration of resulted layouts for the 51dB circuit.

	Optimization	Layout	Area [μm ²]
GDC 51 dB	Traditional		337
	Layout-aware		311

In the first case the area of the resultant layout-aware is smaller than the one obtained by the traditional simulation-based sizing, but in the second case the layout-aware one is bigger. In spite of these different sizings, the traditional sizing might not fulfill all the specifications after

layout because it doesn't account for the physical effects as the layout-aware does. In the next case study the importance of a layout-aware approach will be clearer.

Table 6-6 – Illustration of resulted layouts for 75dB circuit.

	Optimization	Layout	Area [μm^2]
GDC 75dB	Traditional		1021
	Layout-aware		1330

6.2 Case Study II – 2-Stage Folded Cascode Amplifier

In the first case study the main goal was to directly compare the values for the capacitances extracted by AIDA-PEx and Calibre®. In this second example, the goal is to demonstrate how a layout-aware approach with accurate parasitic estimations can be valuable for a correct sizing of the circuit that fulfills all the specifications. The circuit used in the optimization process is the two-stage folded cascode amplifier of Figure 6-3, where the circuit was sized using the traditional optimization-based process and a layout-aware optimization.

The results for the traditional and for the layout-aware optimization are presented in Table 6-7, where the performances for the resulted layouts are simulated using the netlist extracted both from AIDA-PEx and from Calibre®.

In the traditional simulation-based optimization the parasitic effects are not accounted for, and for that reason, when the resulted layout is simulated with the inclusion of circuit's parasitics, the GBW specification is no longer met (whether the circuit is tested on Calibre® or on AIDA-PEx).

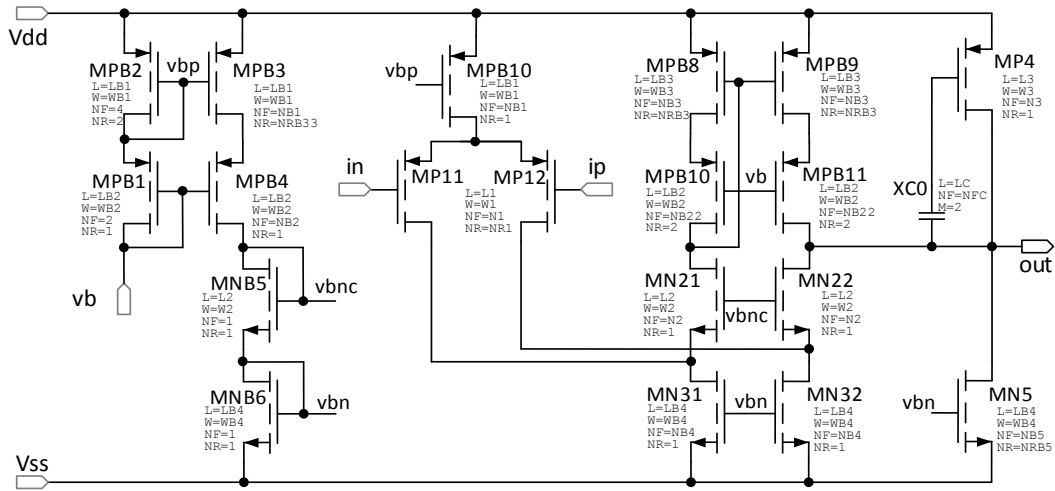


Figure 6-3 –2-stage folded cascode amplifier.

In the layout-aware sizing optimization, the circuit is wittingly over estimated so that when the parasitic components are added the specifications are all fulfilled. In terms of consumption the circuit needs a little more current, consequently increasing the frequency. However, the circuit is correctly sized and the performance measurements from the AIDA-PEx netlist match the ones from Calibre®.

Table 6-7 – Performance Comparison for the traditional and layout-aware optimizations.

Specs		Traditional			Layout-Aware	
		Netlist ¹	AIDA-PEx	Calibre®	AIDA-PEx	Calibre®
Idd	Min [mA]	5.35			5.62	
Gbw	≥ 400 MHz	402.07	392.33	392.59	408.05	408.2
Gdc	≥ 70 dB	73.53	73.53	73.53	75.68	75.68
Area	≤ 20k μm^2	12.09k	16.49k		16.34k	
No	≤ 500 μVrms	197.05	195.37	194.93	195.48	195.16
Pm	≥ 55 °	57.97	55.54	55.26	57.04	56.78
Ov ²	≥ 50 mV	59.48	59.48	59.48	50.61	50.48
D ³	≥ 100 mV	100.33	105.06	105.06	105.37	105.06

¹ - Performance for the netlist excluding parasitics. ² - Overdrive voltage ³ - Saturation voltage

Here, the results have less error than in the previous case study because the circuit is larger and the routing differences are less significant.

In Figure 6-4, both traditional simulation-based optimization and layout-aware synthesis POFs are presented, where the circuit sizings that resulted from the traditional one were tested with parasitic effects to evaluate the post-layout performance. From the resulted layouts, only one held the fulfillment of all the specifications (represented by a circle ○), and all the other sizings became unfeasible, with one or more specifications not fulfilled (represented by a cross ✕). The layout-aware POF, although obtaining layouts with a worse performance, guarantees the entire specification fulfillment for all the resulted circuit sizings.

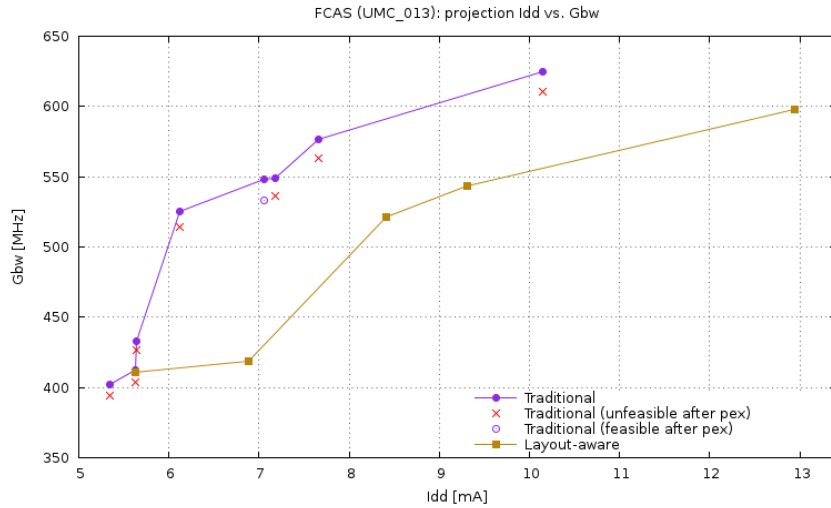


Figure 6-4 – Traditional and Layout-aware optimization POFs (Case Study II).

In Figure 6-5 the resulted layouts for the sizing used in Table 6-7 are illustrated. Although the layouts are alike, the traditional one doesn't fulfill the specifications as the layout-aware one does, due to the inclusion of physical effects in the circuit sizing phase.

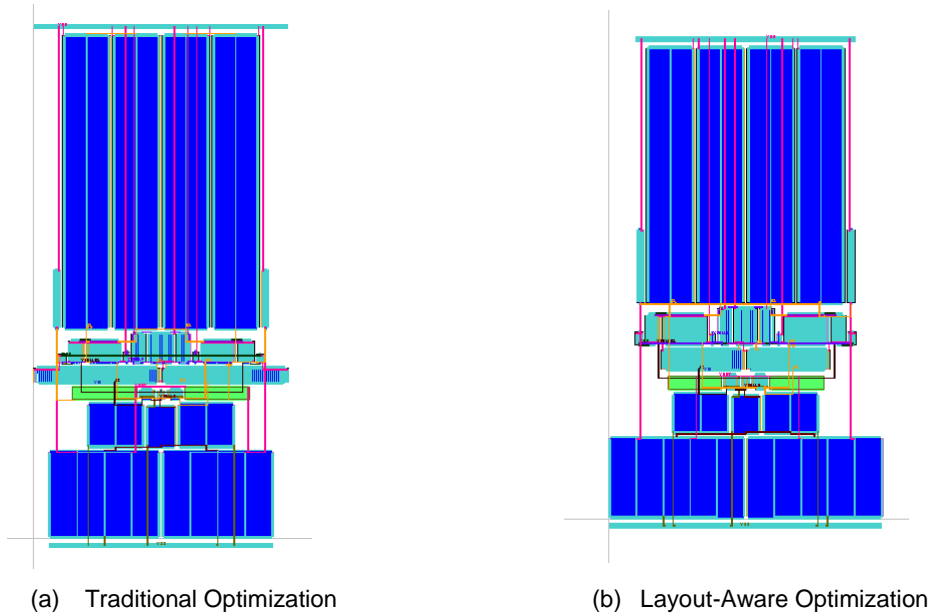


Figure 6-5 –Illustration of resulted layouts (Case Study II).

6.3 Conclusions

In this chapter, two test cases were addressed to show the capabilities of the tool. The first example, a single ended 2-stage amplifier, was used to directly compare the AIDA-PEX extraction results with a standard industry tool, Mentor Graphics Calibre®. The second example,

a 2-stage folded cascode amplifier, was used to demonstrate the importance of the layout-aware synthesis to get a first-right implementation that fulfills all the specification even in the presence of circuit's parasitics.

The results in case study II are better than the previous one, because of the size of the circuit, where the components are larger than the first one. In terms of circuit's parasitics, these have a bigger effect, and the parasitic components have larger values. However, the error between the extracted values from AIDA-PEx and Calibre® are smaller because the difference in the layouts extracted by these tools (routing paths) is less significant to the final parasitic extractions.

Chapter 7 Conclusions and Future Work

This chapter presents the closing remarks, and then, the future directions for the continuous development of AIDA-PEx are outlined.

7.1 Conclusions

The proposed methodology for layout-aware analog IC sizing was proved by the implementation of a tool, AIDA-PEx, that enables the layout generation block to retrieve the layout-related data (geometrical characteristics, parasitic components, etc.) fast enough to have acceptable running times. AIDA-PEx outstands from the remaining tools presented in the state-of-the-art (Chapter 2), addressing some drawbacks by obtaining a complete empirical based 2.5-D parasitic extraction with approved results when compared to a commercial tool widely accepted in the industry, Calibre®.

By merging the circuit optimizer with the layout generator (AIDA-C and AIDA-L), this layout driven approach includes layout-related data in early stages of the optimization, with an innovative solution for parasitic estimation of interconnect and substrate capacitance and global routing in-loop for each different sizing solution. The lightweight built-in extractor estimates the impact of layout parasitics for both floorplan and early-stages of routing without requiring a detailed layout, greatly reducing overall evaluation time to in parasitic-aware optimization.

The tool relies on new regression on the technology related data retreated from the TDK, as well as new computing and modeling of the interpolated data to accurately estimate the circuit's parasitics. Additionally, new geometrical factors are considered in the capacitance modeling, which along with the formulations developed, result in an overall precision of the proposed approach compared with already accepted tools.

In Chapter 6 two case studies were presented to validate the tool. In the first one, the results showed sufficient accuracy for the proposed extractor, with errors below 40% for direct capacitance comparison with Calibre®. In the second case study, the importance of the layout-aware circuit sizing was verified, with almost 90% of the traditional optimization solutions turning unfeasible after post-layout simulation. For this experiment, the results showed an outstanding precision, with relative errors not exceeding 1%.

7.2 Future Work

The conducted experimental tests were presented for the UMC 0.13 μ m design process, although the formulations for the estimation of circuits' parasitics would also work for other technologies, if the provided TDKs matched the desired technology. In the development of this

work only the UMC 0.13 μ m design kit was available, but for future reference the validation of the modeling applied for other technologies would empower the tool.

In order to accelerate even more the extraction process, a solution of parallel computing could be studied to be implemented in the tool. The extractor is fast, but for large circuits, if various parts of the circuit could be analyzed at the same time, it would optimize the total runtime for an even quicker estimation.

The frequency of operation of the circuits tested in this work rounds the hundreds of MHz. The larger the value of the frequency, the more effect the parasitic components have in the final circuit's performance. The radio-frequency (RF) circuits can operate within a range of about 3kHz up to 300GHz, where if the parasitic effects are not accurately modeled, the estimated performances will be different from the real ones, which can even lead to a total loss of the initial constraints implied. The application of this extractor for RF circuits would challenge the accuracy of the estimated and force the tool to be more robust.

AIDA-PEx project is not closed, far from it, this work served to validate the concept and it provides support for further developments. New people will bring new insights in the analog IC layout generation problem, and it is hoped that AIDA will converge to an application suitable for industrial uses.

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